

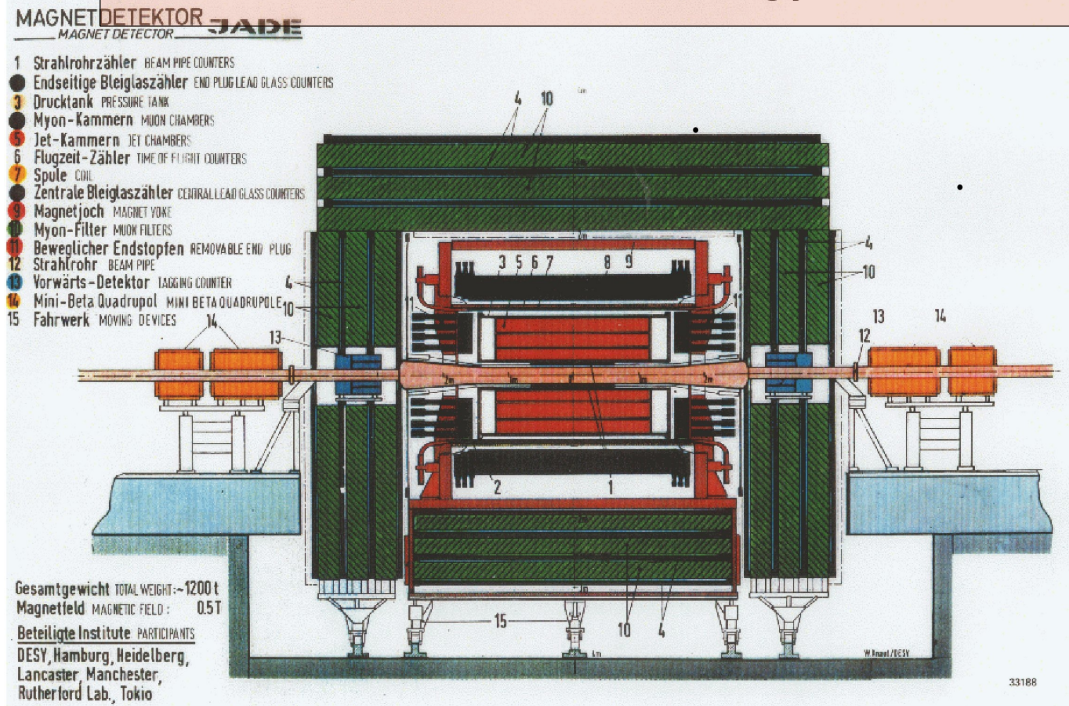
Determinations of α_s and tests of analytic hadronisation models using e^+e^- annihilation data.

S. Bethke, O. Biebel, S. Kluth, C. Pahl*, J. Schieck and the JADE Collaboration

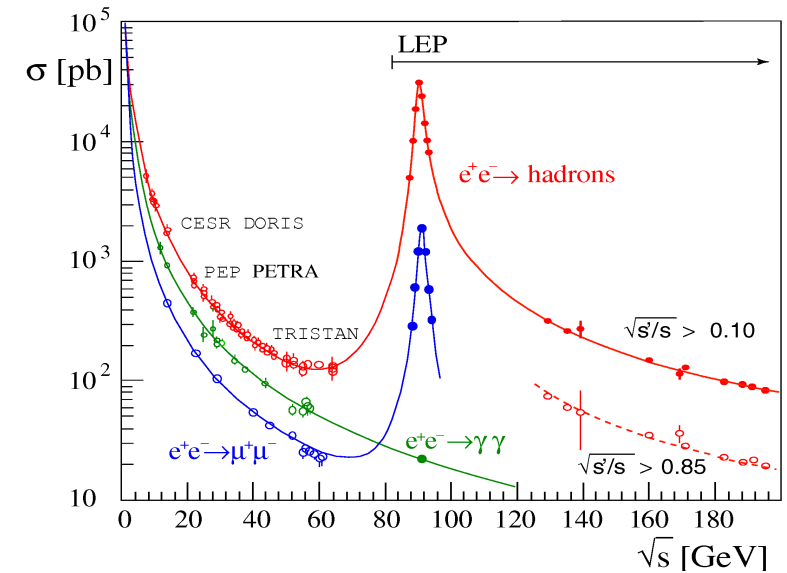
- JADE experiment
- Event shape distributions and moments
- Analysis of moments from JADE and OPAL using analytic hadronisation models ([arXiv:0904.0786](#))
- Measurement of α_s from JADE distributions using new NNLO calculations ([arXiv:0810.1389](#))
- Conclusion and outlook

JADE Experiment, 1978-1986

At PETRA, DESY, c.m. energy $Q=12-44\text{GeV}$

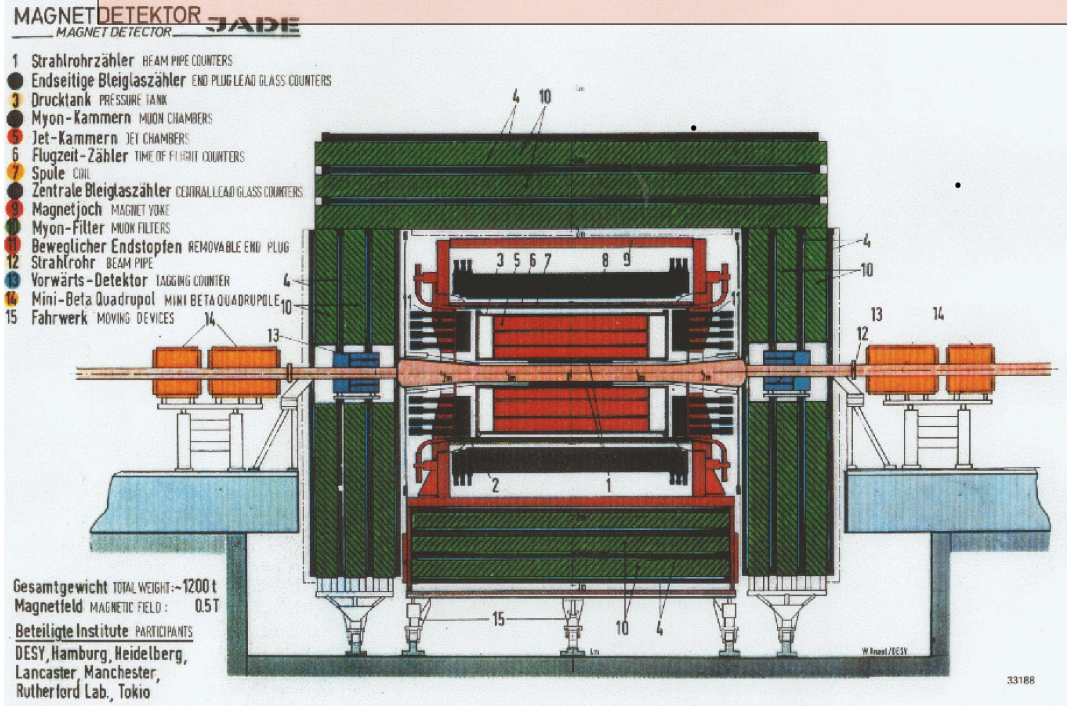


hadronic cross section

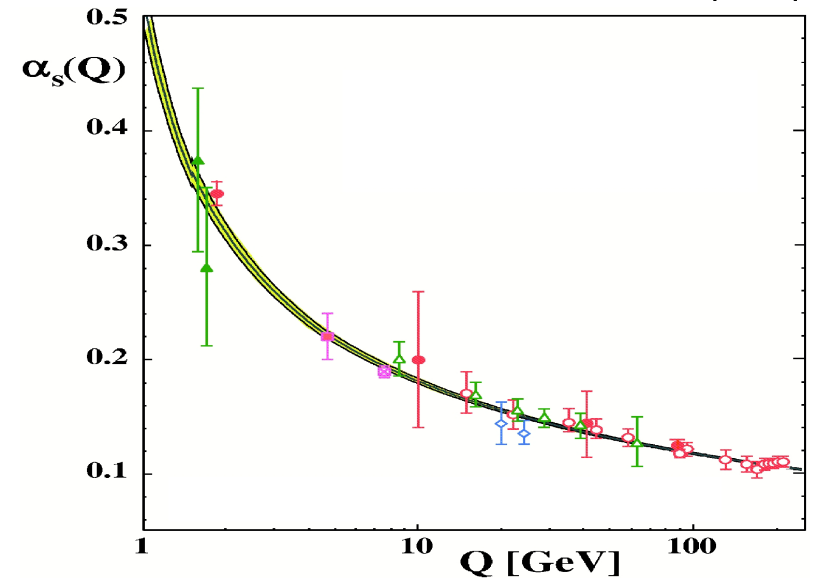
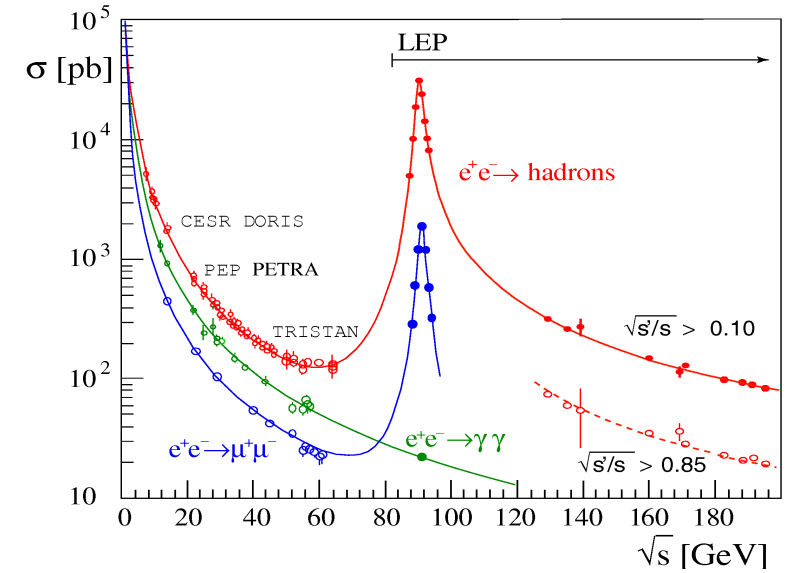


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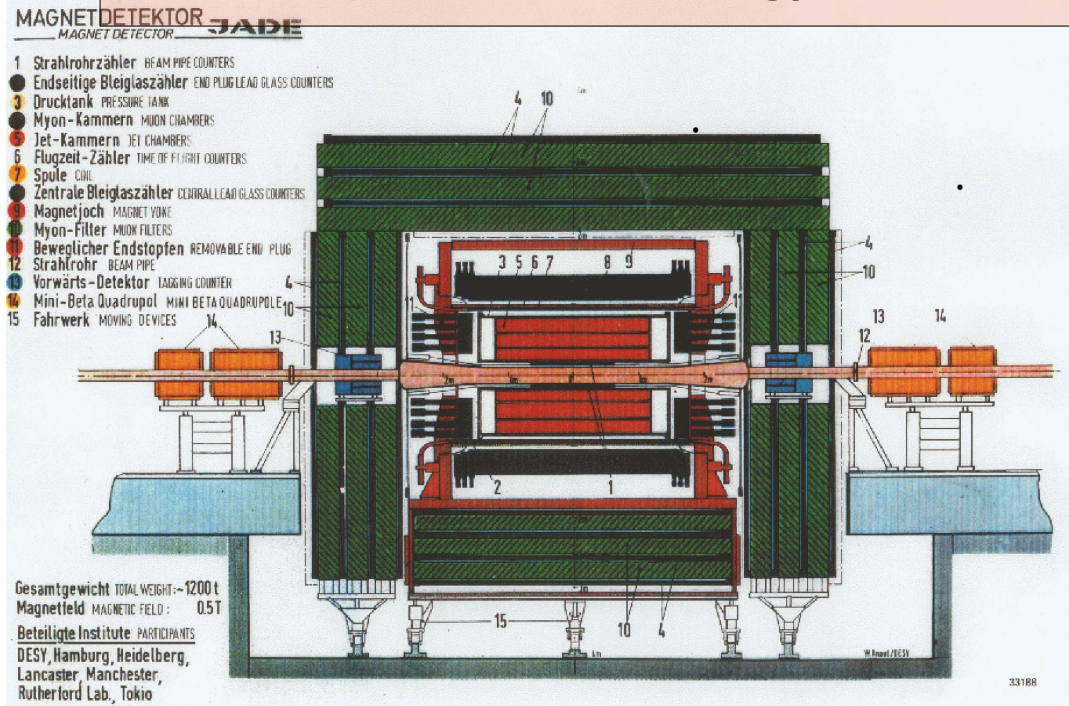
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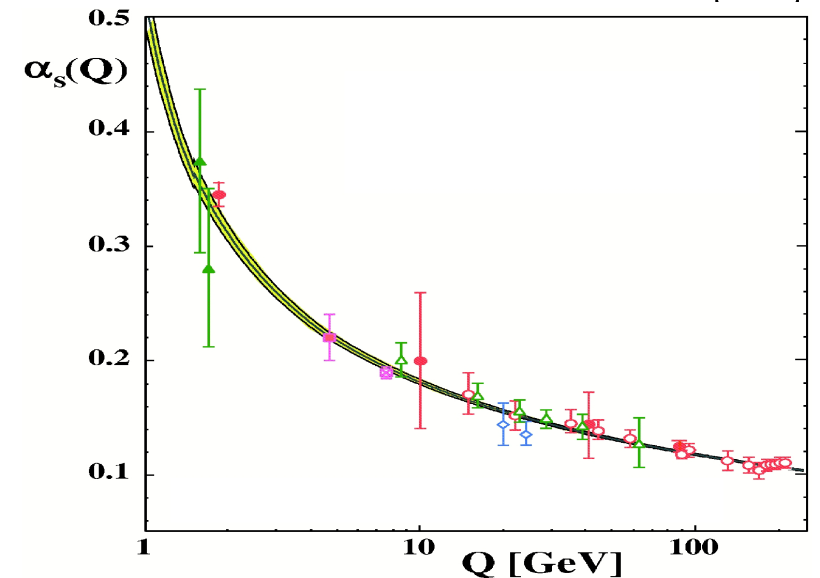
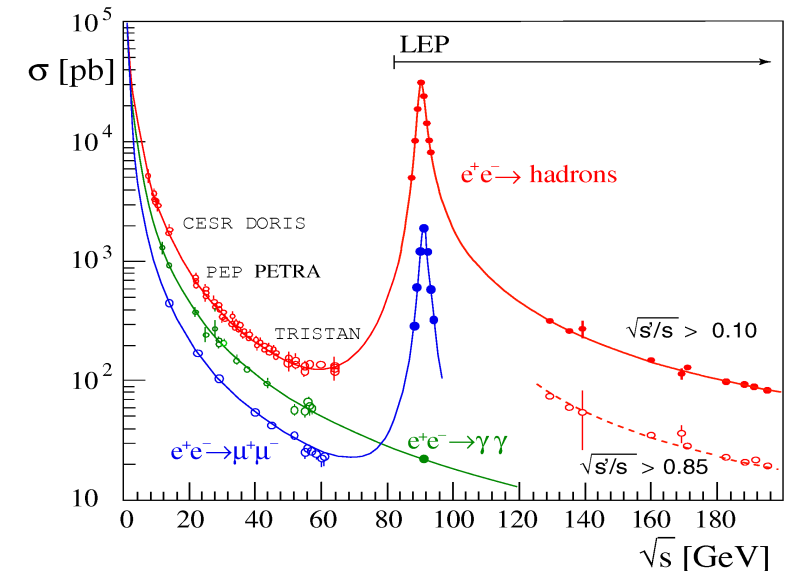
- QCD effects stronger at low Q

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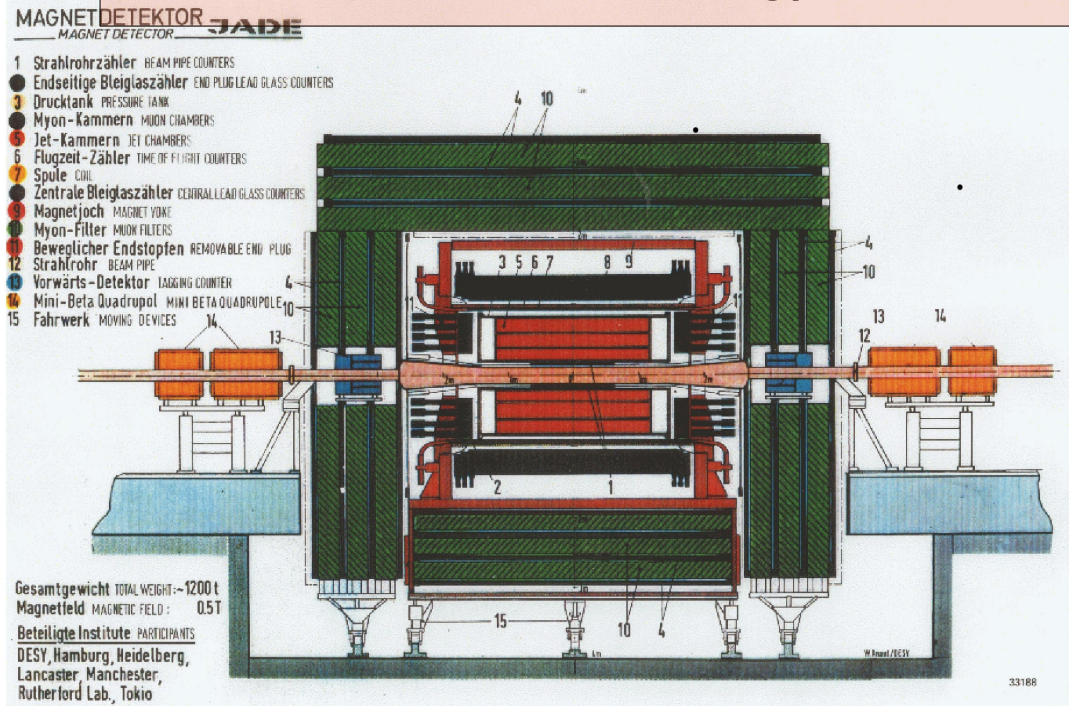
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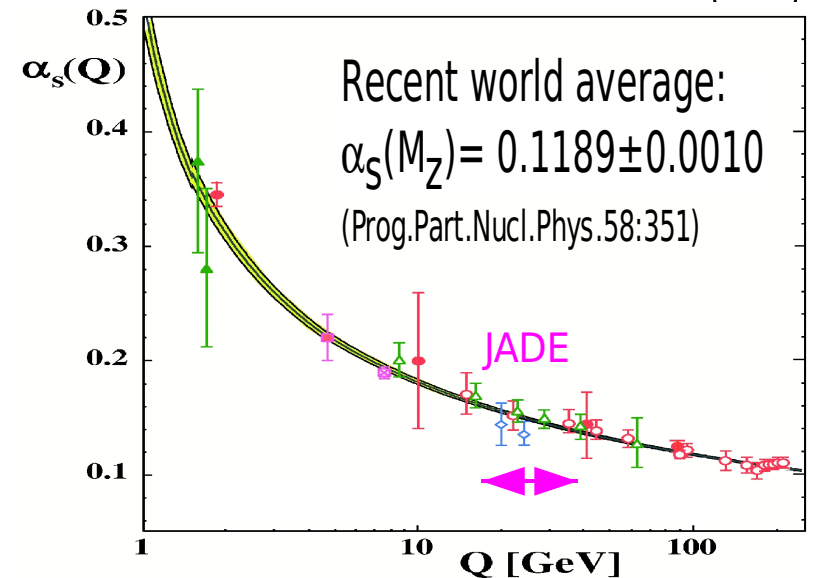
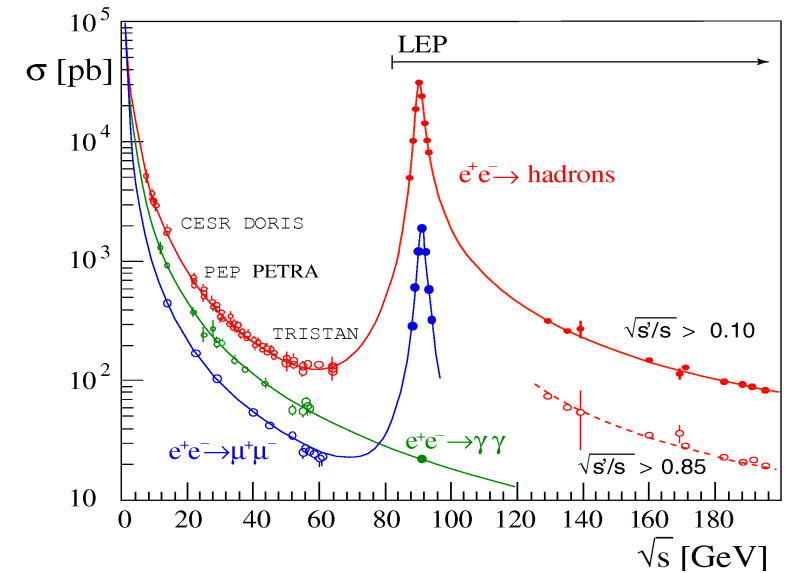
- QCD effects stronger at low Q
- Old data saved from tapes, printouts.
- Analysis and detector simulation software reactivated
- New Monte Carlos, new calculations

JADE Experiment, 1978-1986

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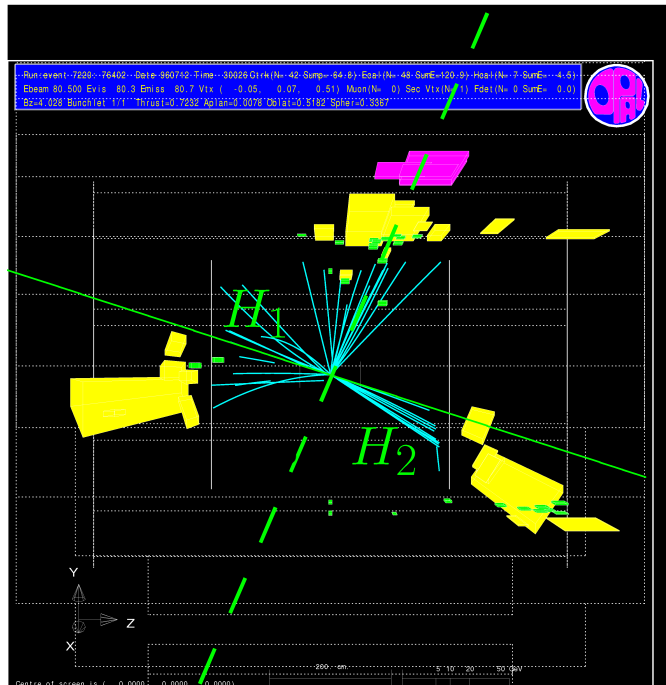
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Event shape variables y

- Thrust $1-T$
- C-parameter
- Total Jet Broadening B_T



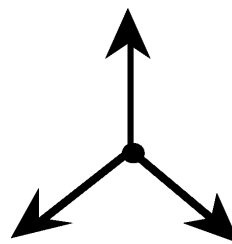
- Wide Jet Broadening B_W
- Durham two-jet flip parameter y_{23}^D
- Heavy Jet Mass M_H

(Two-hemisphere variables)

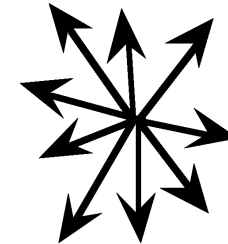
(One-hemisphere variables)



qq: 2 Jets, $y \approx 0$



qqg: 3 Jets, e.g. $1-T \approx 1/3$

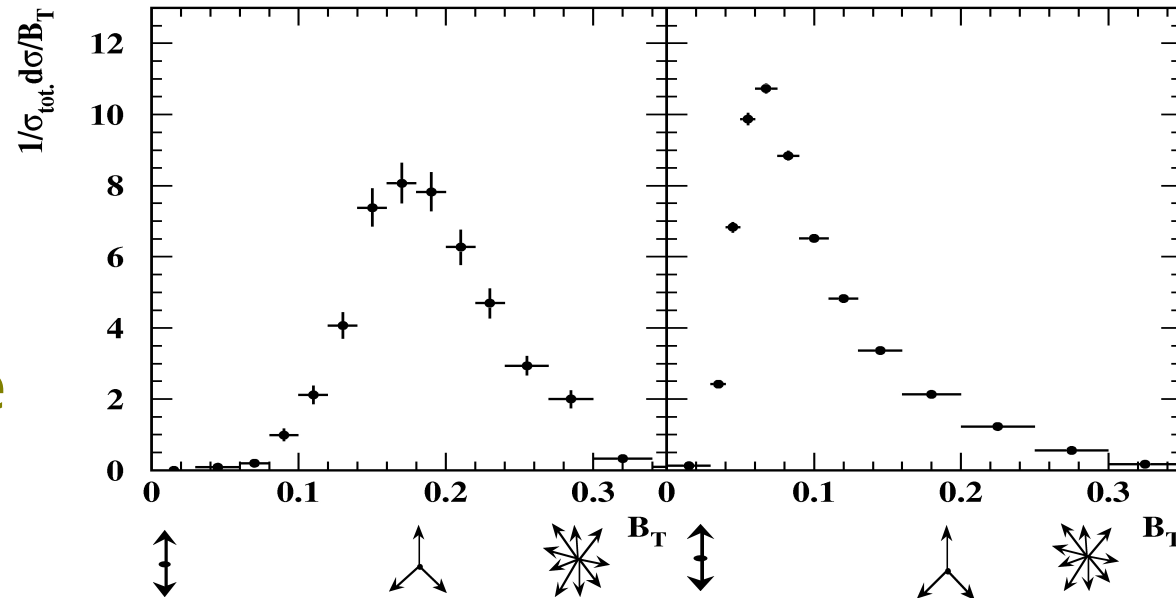


Many gluons, e.g. $1-T \approx 1/2$

Distributions and moments

- Distributions

B_T at
14 GeV:
 α_s large

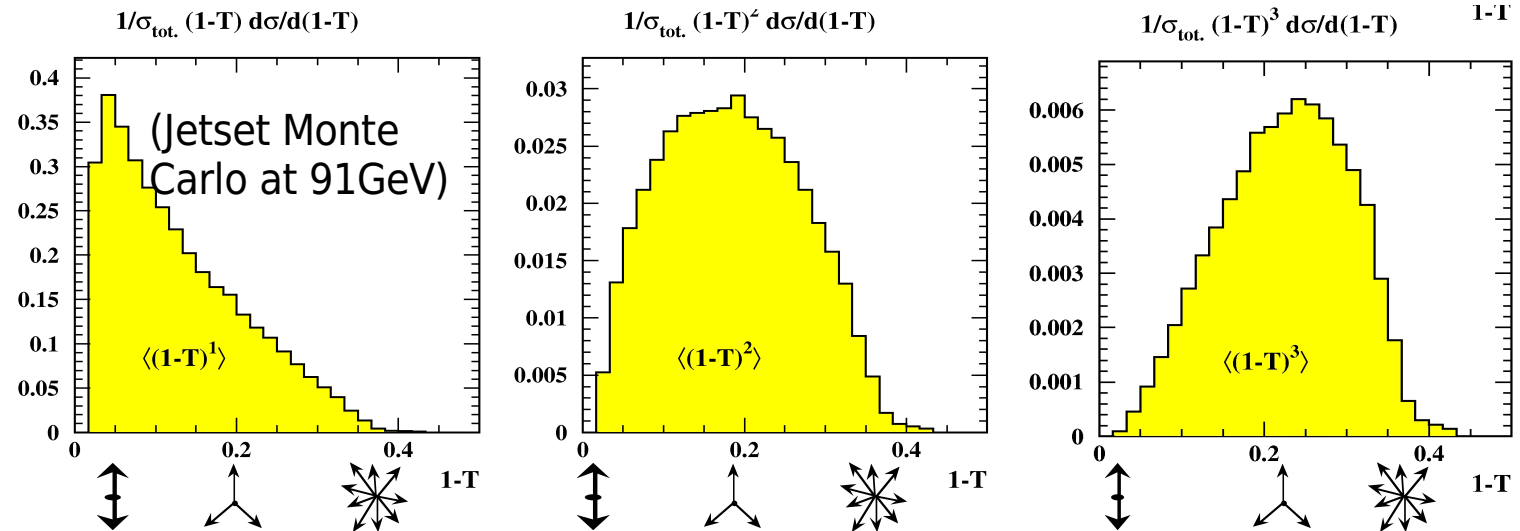


B_T at
91 GeV:
 α_s small

- Moments

$$\langle y^n \rangle = \int y^n \frac{1}{\sigma} \frac{d\sigma}{dy} dy$$

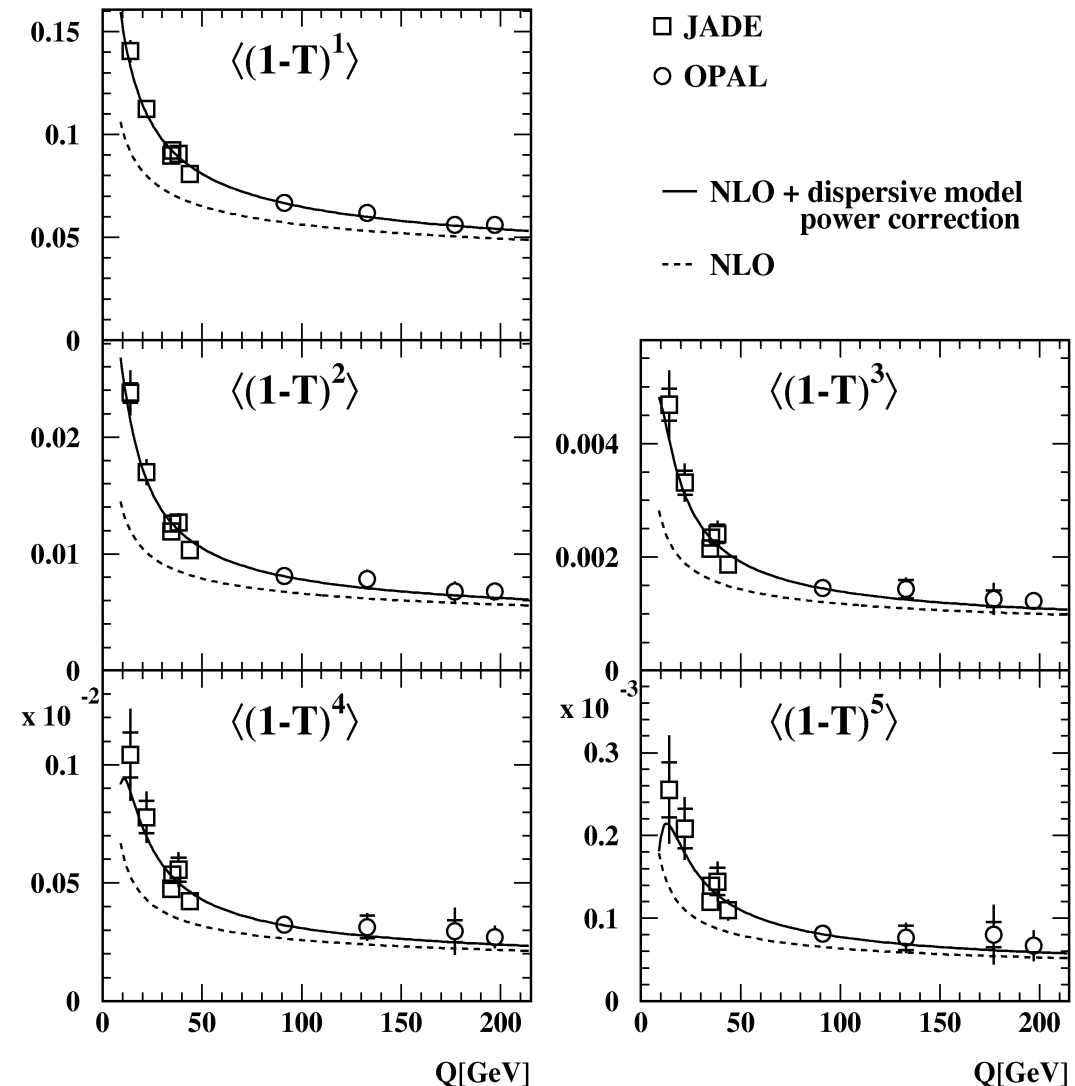
Higher order
moments probe the
multi-jet region:



Testing QCD: Fits to the moments

- $\langle y^m \rangle$, $m=1\dots 5$ measured by JADE and OPAL
- Hadronisation correction by **analytical “non perturbative” power correction models**
- Perturbative predictions: **Next to Leading Order**,
$$\langle y^n \rangle = A_n \alpha_s(Q^2) + B_n \alpha_s^2(Q^2)$$

Fits to moments of Thrust on hadron level

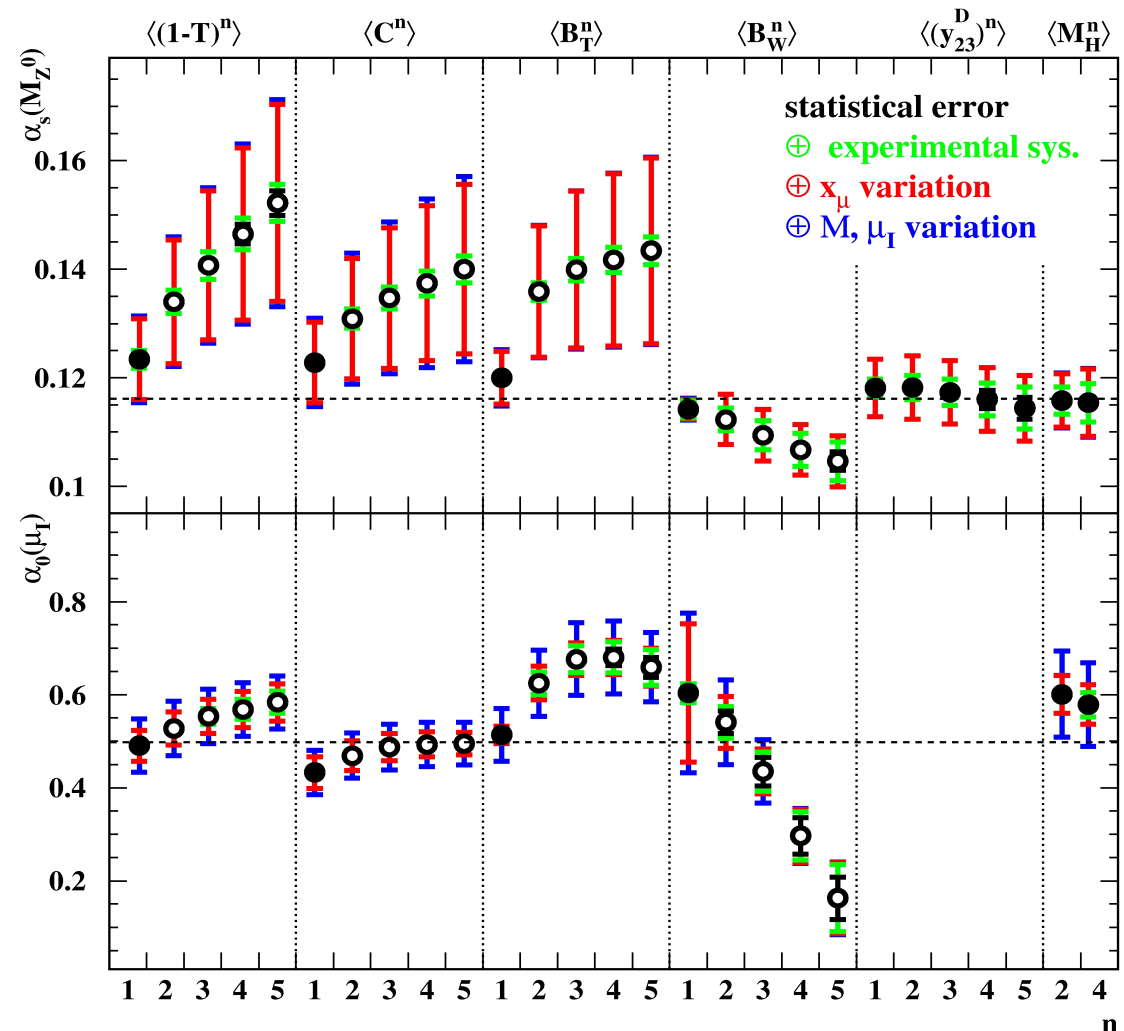


Testing QCD: Fits to the moments

- Dispersive model (Dokshitzer et al.):

$$\frac{d\sigma_{had.}}{dy} = \frac{d\sigma_{pt.}}{dy} (y - a_y * P(\alpha_0))$$

Dispersive model: Measurements of $\alpha_S(M_Z)$ and α_0



Testing QCD: Fits to the moments

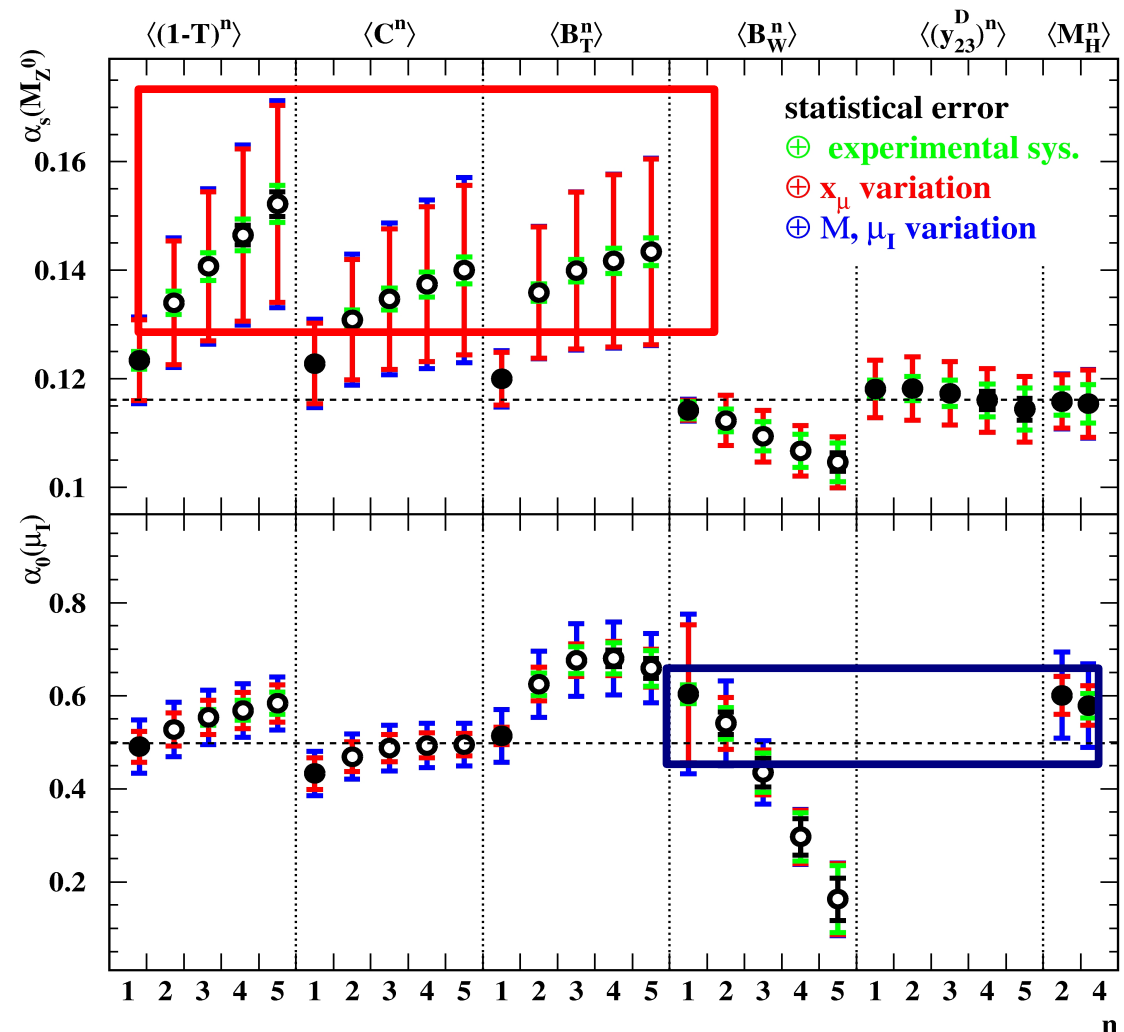
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Deficiencies of the NLO predictions lead to non universalities of the fit parameters:

- Significant rise of $\alpha_S(M_Z^0)$ with moment order n for two-hemisphere moments
- higher α_0 for one-hemisphere moments

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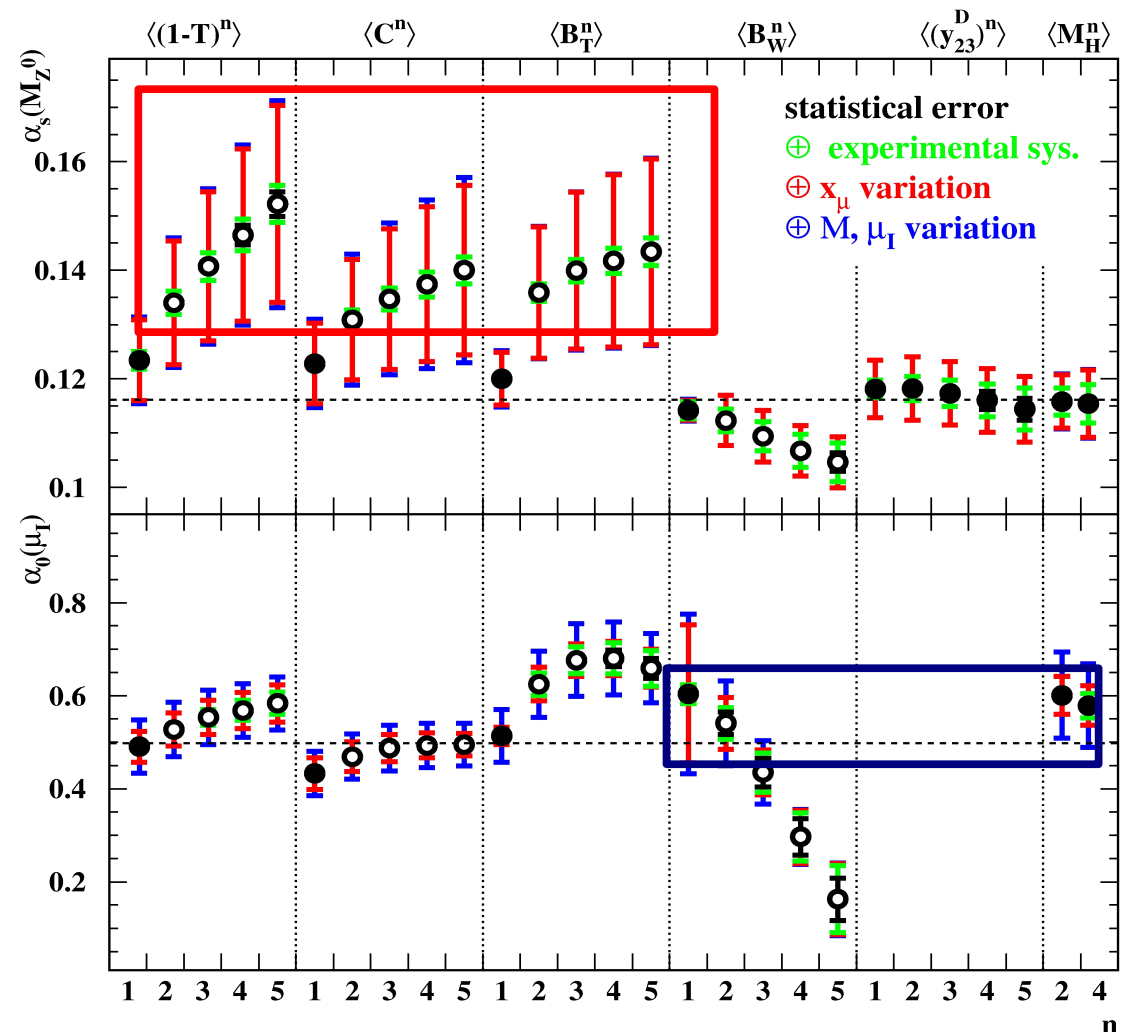
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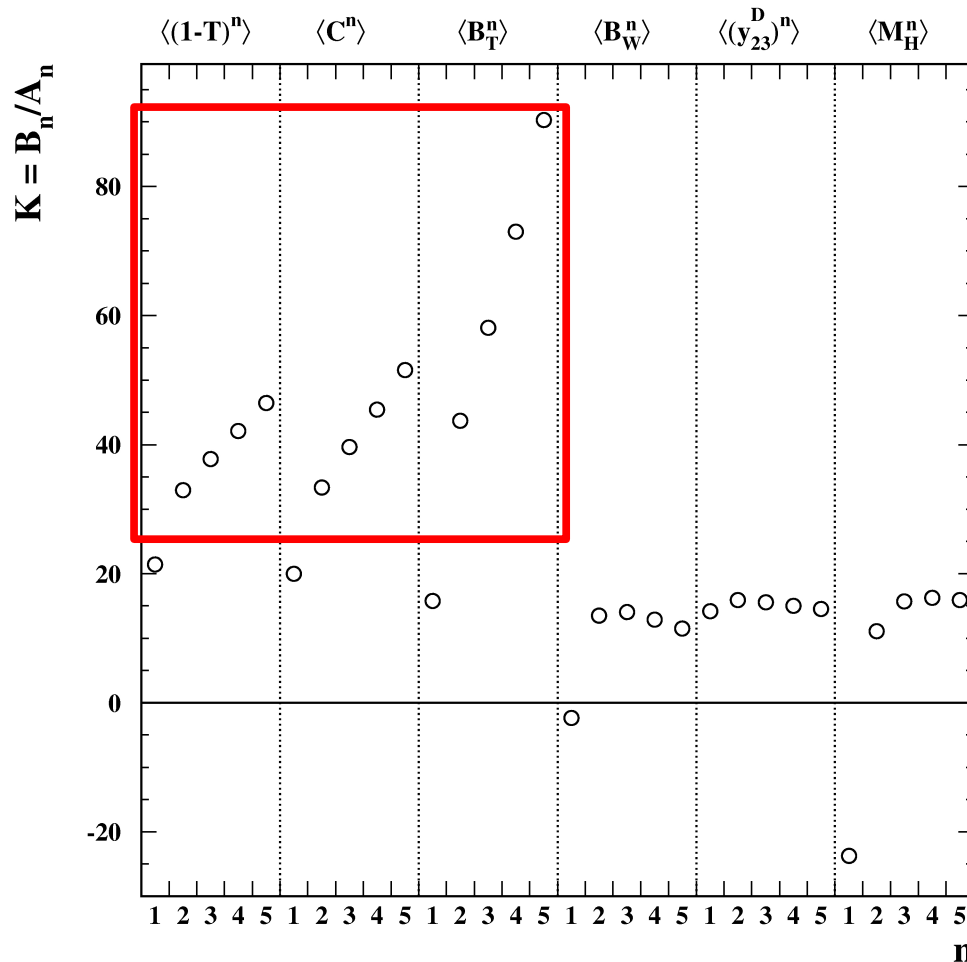
- Shape Function (Korchemsky)
- Single dressed gluon approximation (Gardi et al.):
 $\alpha_S(M_Z) = 0.1172 \pm 0.0036$

Dispersive model: Measurements of $\alpha_S(M_Z)$ and α_0



Testing QCD: Fits to the moments

Predictions: $K = B_n / A_n$



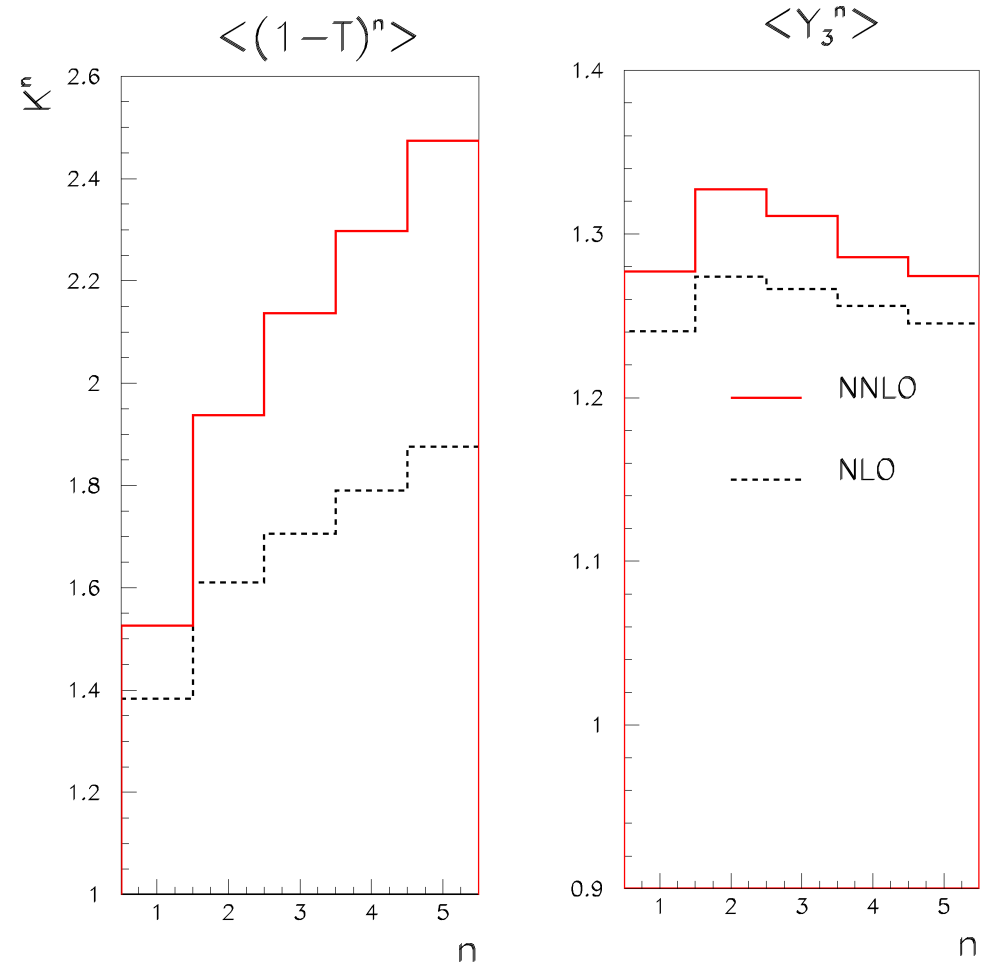
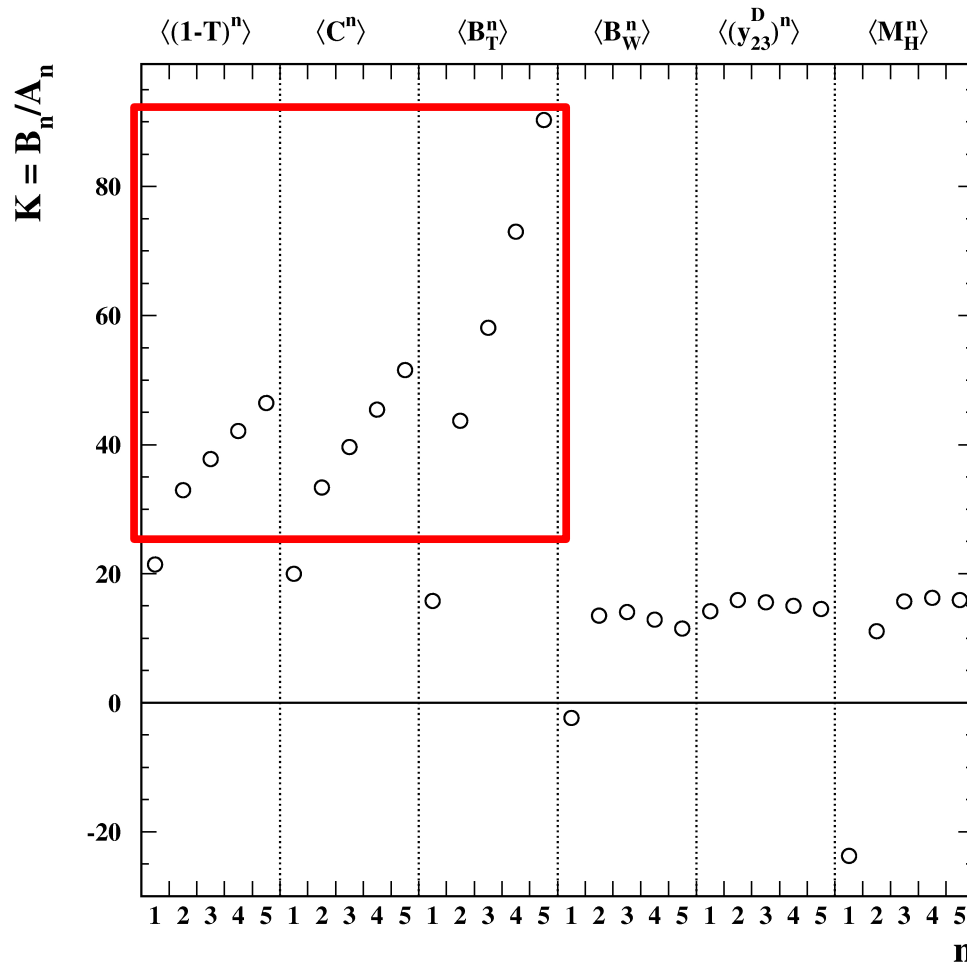
NLO calculations: Two-hemisphere moments receive large corrections in α_s^2 .

Fit results: Trend seems to continue...

Testing QCD: Fits to the moments

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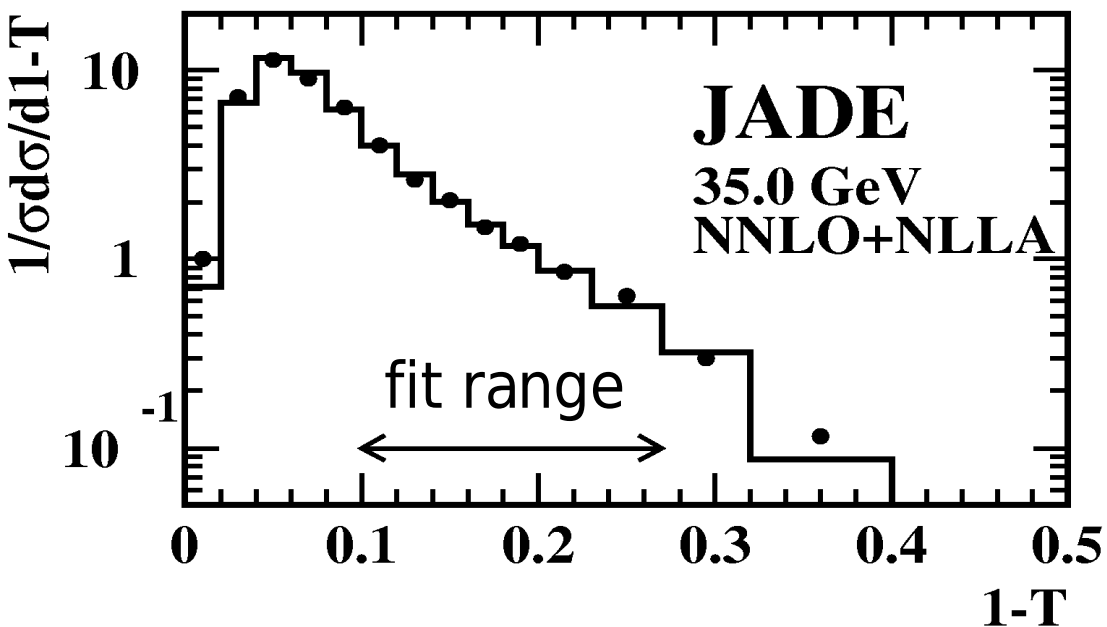
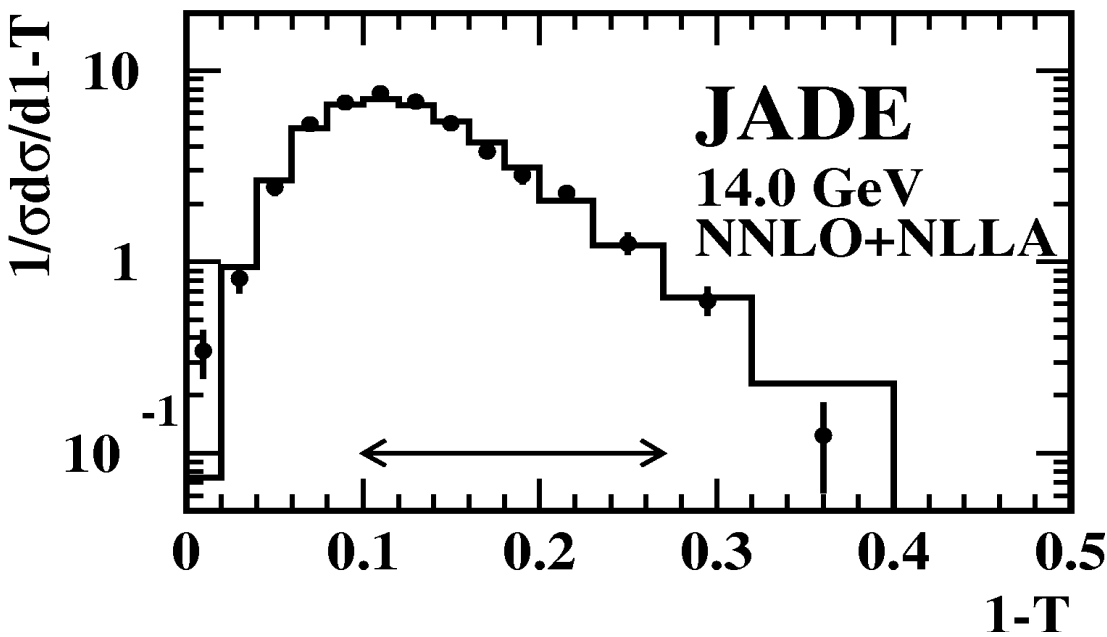
NNLO/LO



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New: Theoretical explanation (JHEP 0905:106, 2009)

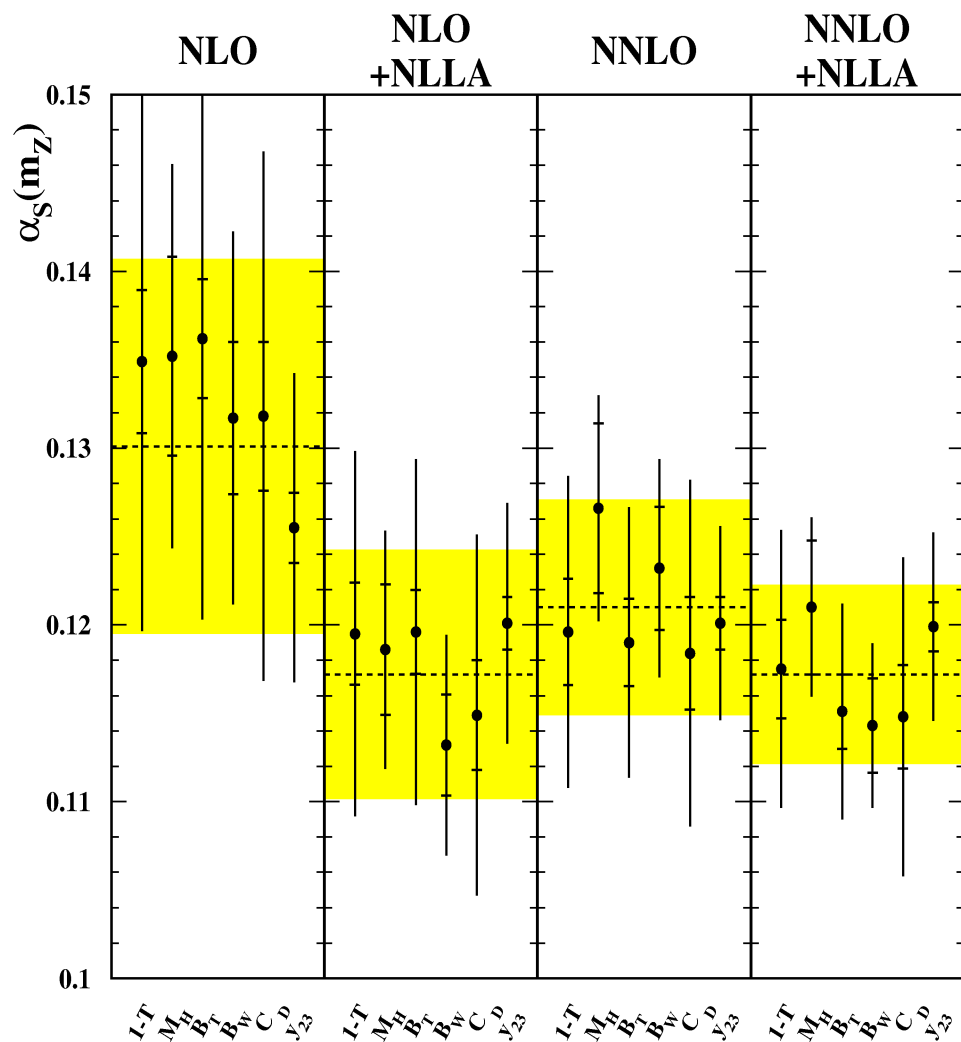
Measuring α_s : New NNLO calculations



- Predictions: **N**ext to **N**ext to **L**eading **O**rders $O(\alpha_s^3)$ (finished 2008 after 25 years) + **N**ext to **L**eading **L**ogarithmic **A**pproximation
- Hadronisation correction by **M**onte **C**arlo **m**odels
- More complete than NLO analyses: Data described well over virtually all phase space

Measuring α_s : New NNLO calculations

$\alpha_s(m_{Z^0})$ results



- More complete than NLO+NLLA analyses:
 - renormalisation scale uncertainty reduced
 - scatter from different variables reduced
- Result from JADE, NNLO+NLLA:

$$\alpha_s(M_{Z^0}) = 0.1172 \pm 0.0051$$

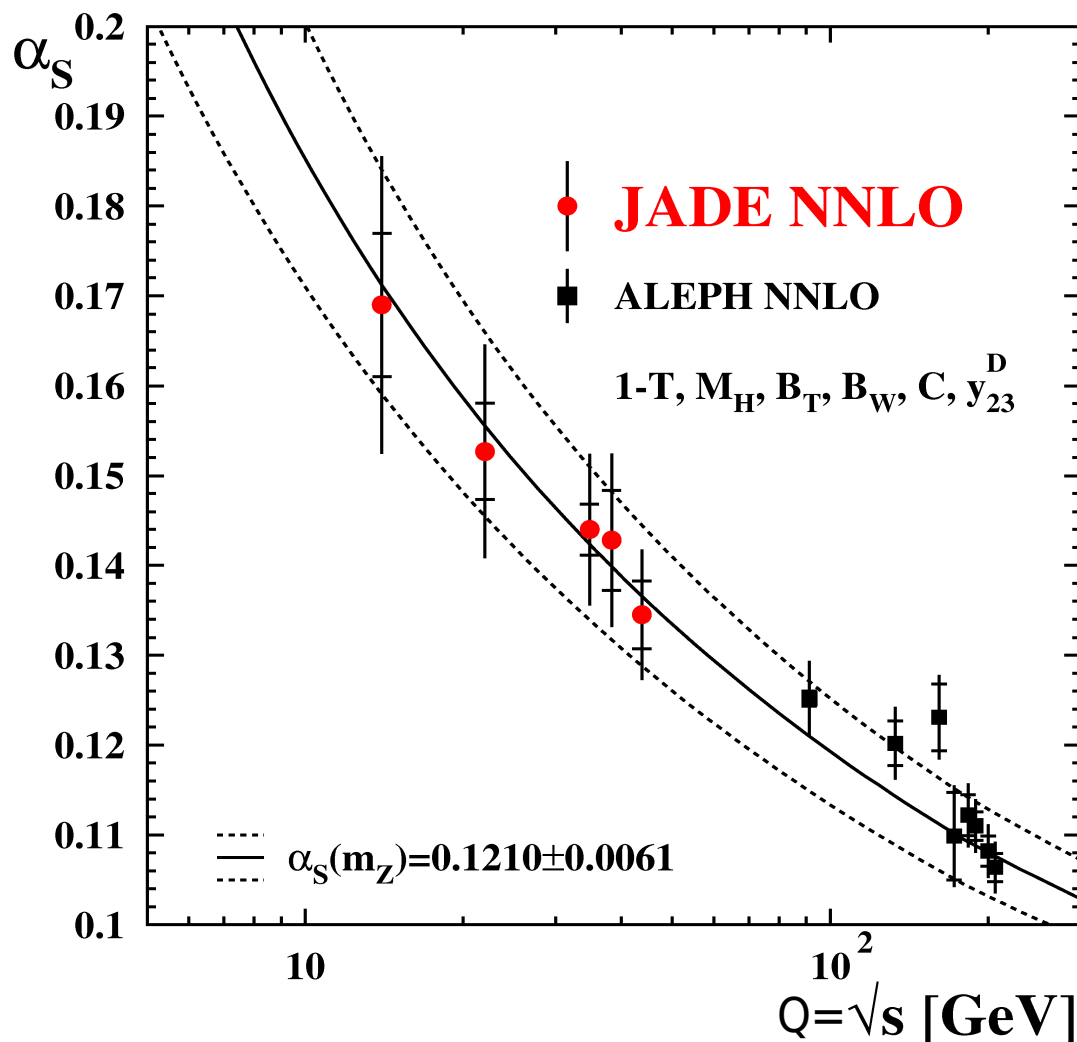
4% precision, among the best measurements

Errors: stat. / exp.+had.+scale

Measuring α_s : New NNLO calculations

Running $\alpha_s(Q)$ result

from event shape combination



Running of α_s confirmed strongly in the JADE range 14—44 GeV.

NNLO: $\alpha_s(m_{Z^0}) = 0.1210 \pm 0.0061$ (tot.)
NNLO+NLLA: $\alpha_s(m_{Z^0}) = 0.1172 \pm 0.0051$ (tot.)

Errors: stat. / exp.+had.+scale

Conclusion

- Running of $\alpha_s(Q)$ confirmed strongly in the JADE energy range
- $\alpha_s(m_{Z^0})=0.1172\pm 0.0051(\text{tot.})$ from NNLO+NLLA at 14-44 GeV
- Event shape moments reveal shortcomings of the NLO calculations
- Outlook:
 - OPAL NNLO analysis in progress
 - Moments NNLO analysis would be interesting
 - Re-analyses of data taken at the JADE and OPAL experiment have huge potential
 - QCD precisely studied in e^+e^- important for LHC