

*Jet Physics in
 $e^+ e^-$ Annihilation
from 14 to 209 GeV*

QCD '03, Montpellier, 02.07.03

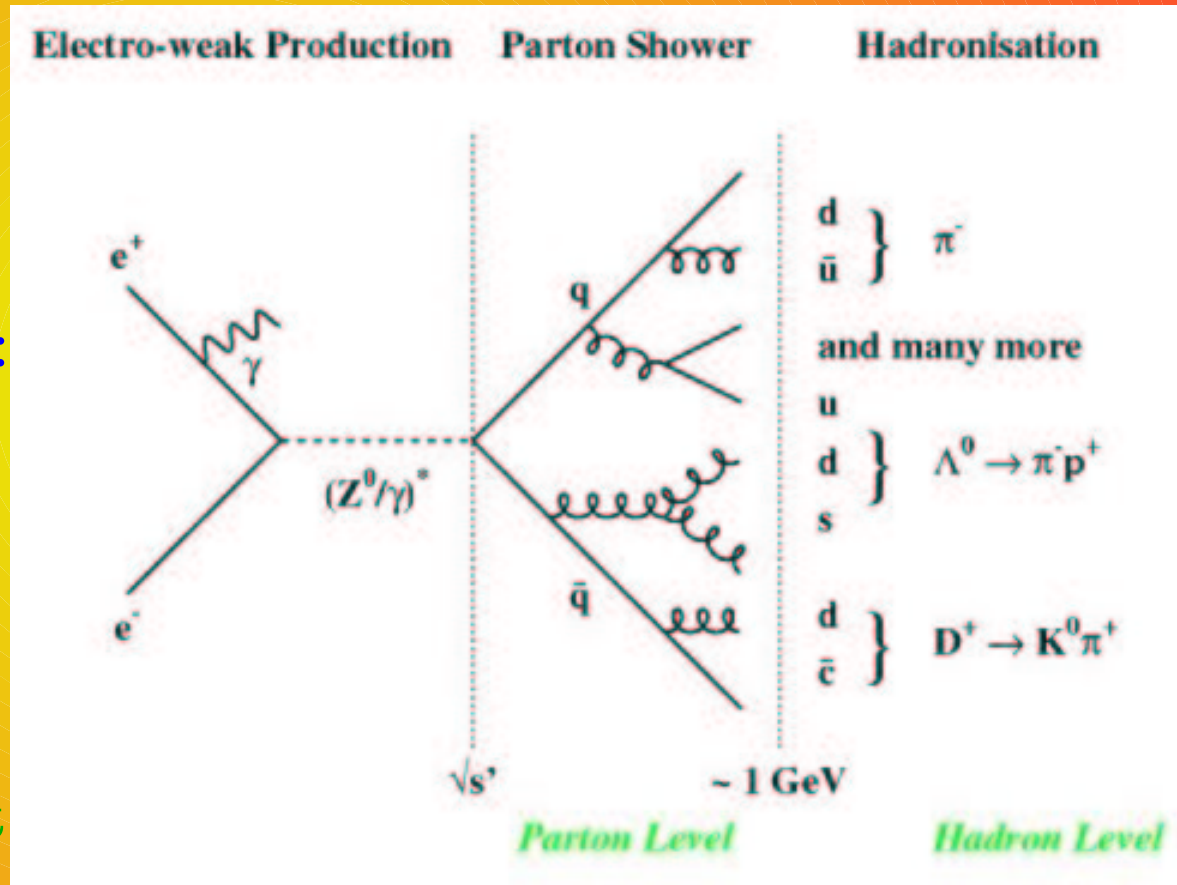
- 1 Introduction
- 2 Hard QCD
- 3 Gauge Structure
- 4 Conclusions/Outlook

Stefan Kluth
Max-Planck-Institut für Physik
Föhringer Ring 6
D-80805 München
skluth@mppmu.mpg.de

1 Introduction

Hadron production in e^+e^- annihilation is ideal laboratory for QCD studies:

- no interference between initial and final states
- maximal energy in laboratory system
- no p.d.f.s to worry about



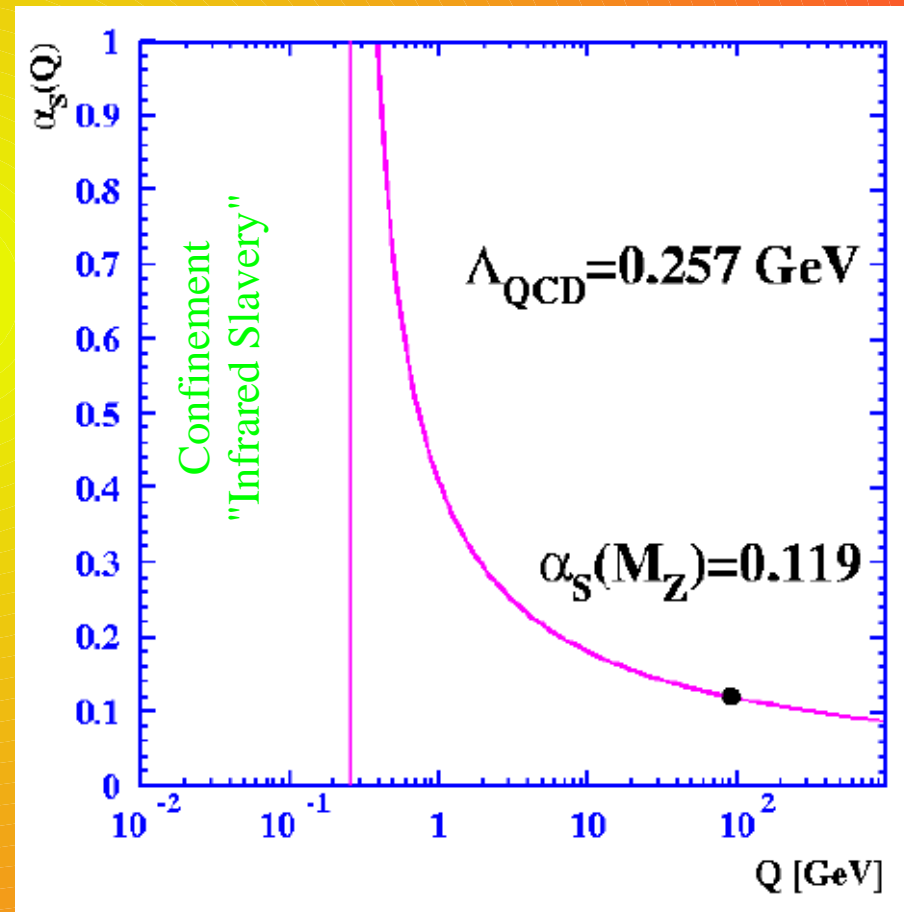
1 Running coupling "constant"

$$\alpha_S(Q) = \frac{\alpha_S(\mu)}{1 + \beta_0 \alpha_S(\mu) \ln(\mu^2/Q^2)}$$

$$= \frac{1}{\beta_0 \ln(Q^2/\Lambda_{QCD}^2)}$$

$$\beta_0 = (11 C_A - 2 n_f) / (12 \pi)$$

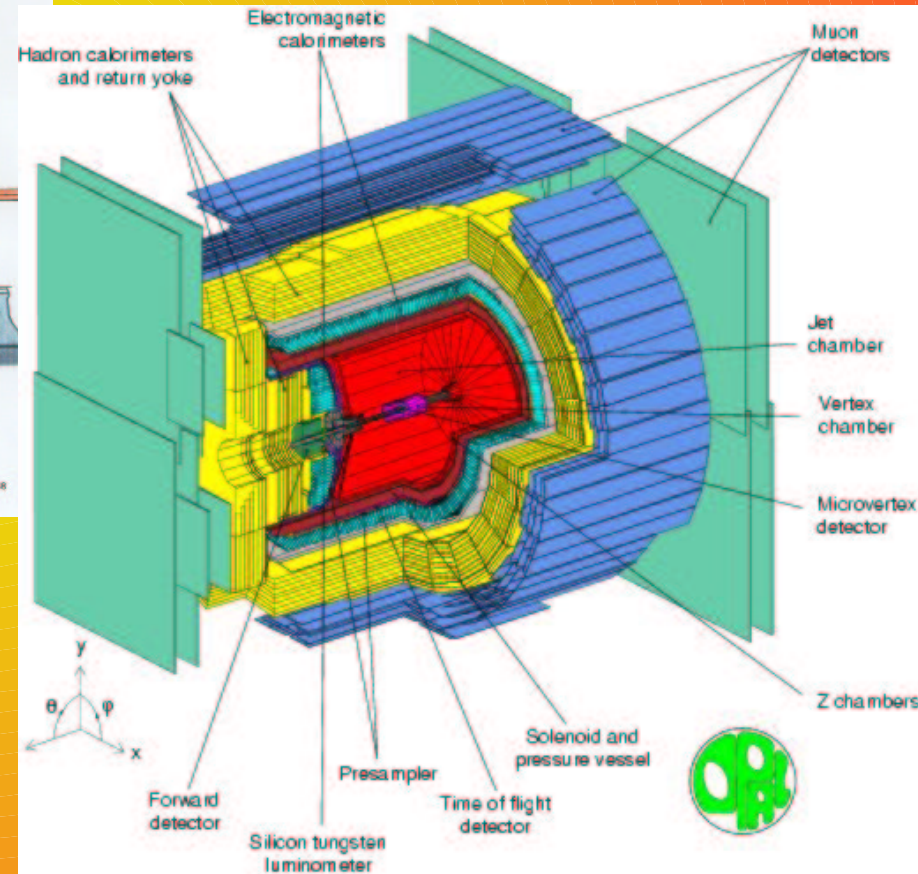
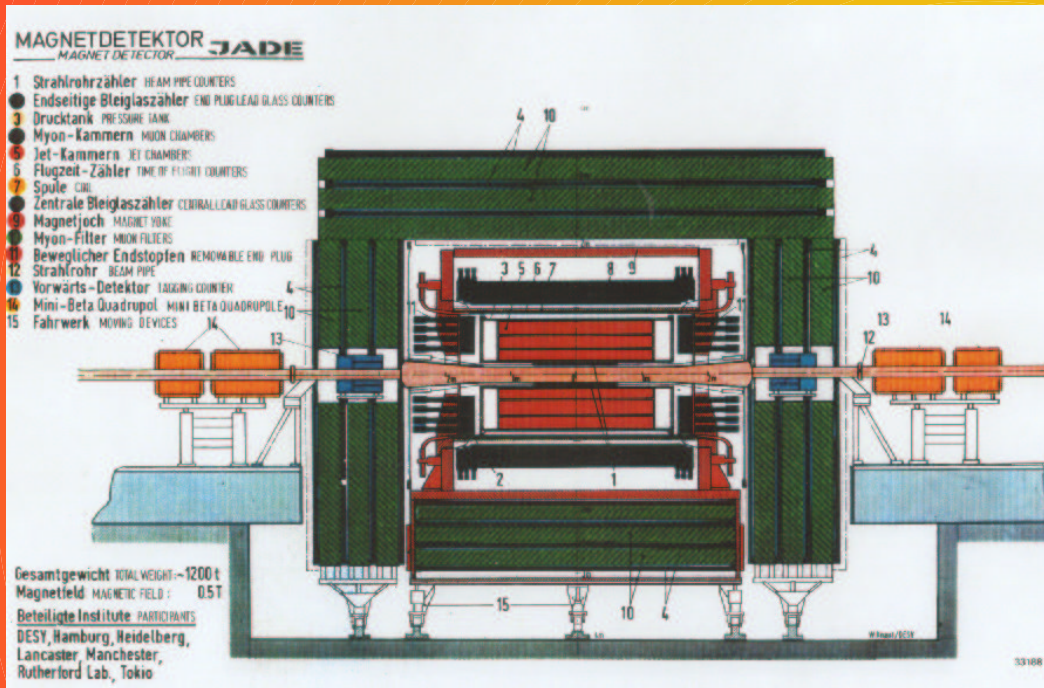
- Strong coupling "constant" runs
- Divergence at small Q,
the "Landau pole"
- "Asymptotic freedom" means that
 $\alpha_S(Q)$ vanishes for infinite Q



1 "QCD Experiments"

OPAL: 1989 to 2000 at LEP
(CERN)

$\sqrt{s} = 88$ to 209 GeV

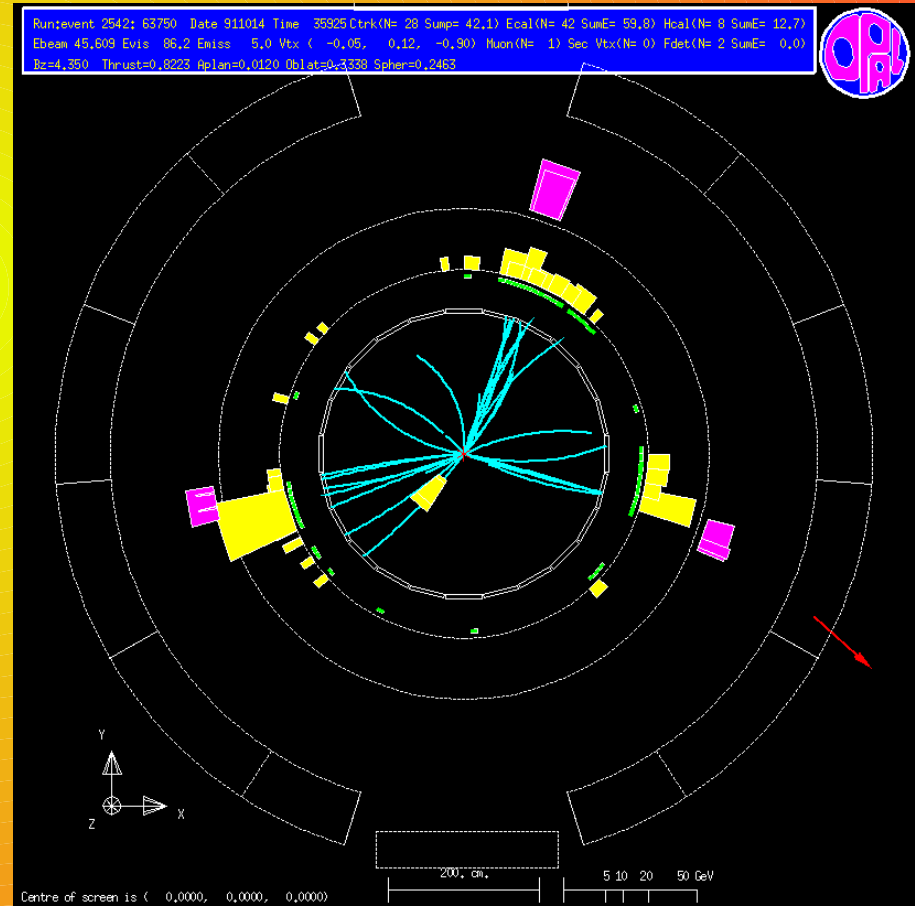
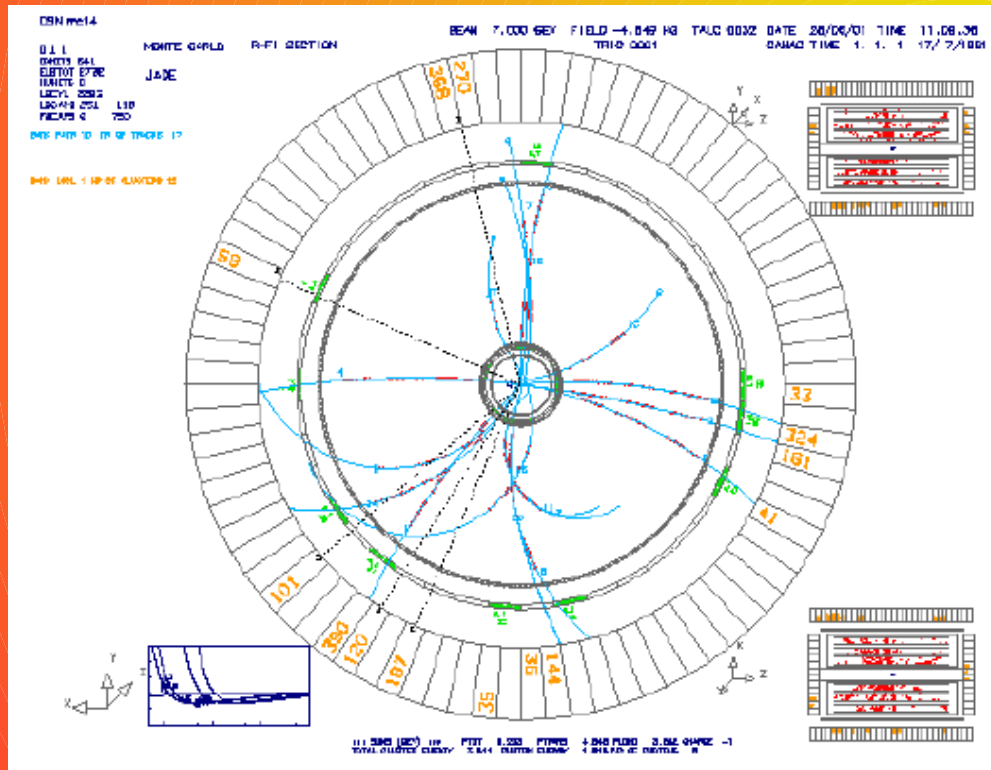


JADE: 1979 to 1986 at
PETRA (DESY)
 $\sqrt{s} = 14$ to 44 GeV

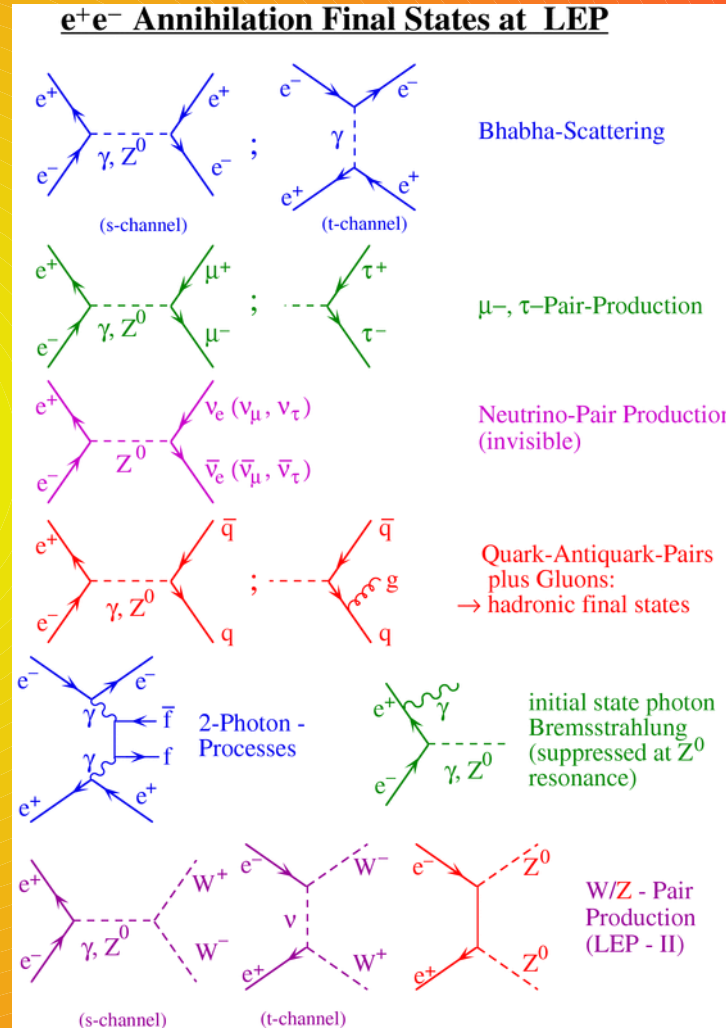
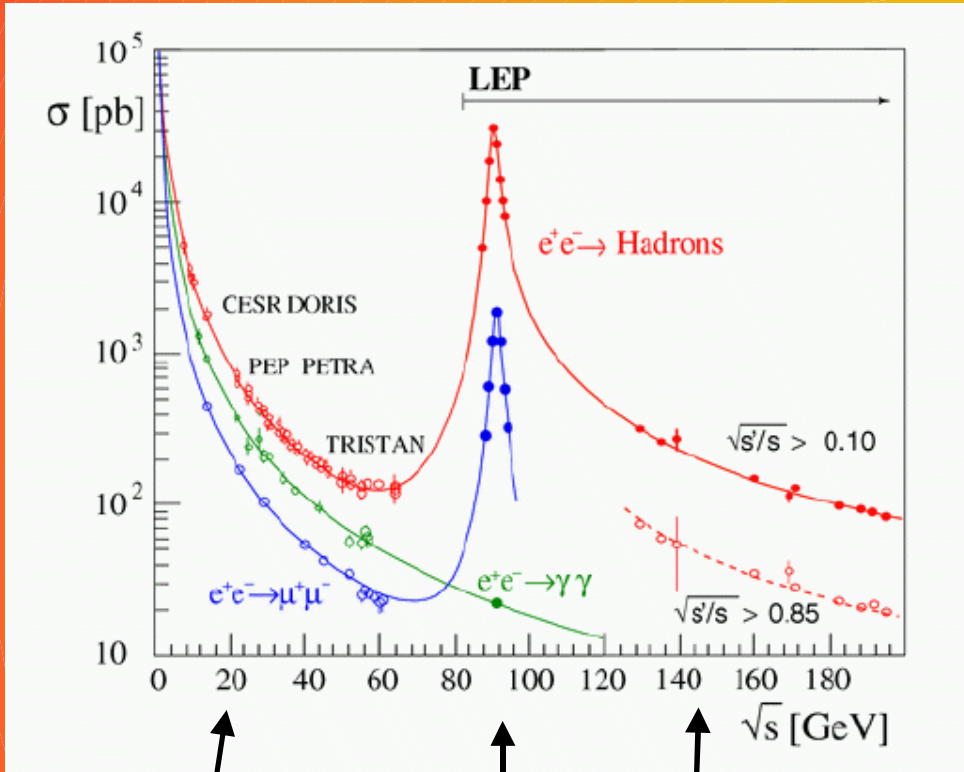
1 QCD Events

JADE $\sqrt{s} = 14 \text{ GeV}$

OPAL $\sqrt{s} = 91.2 \text{ GeV}$



1 Event Selection

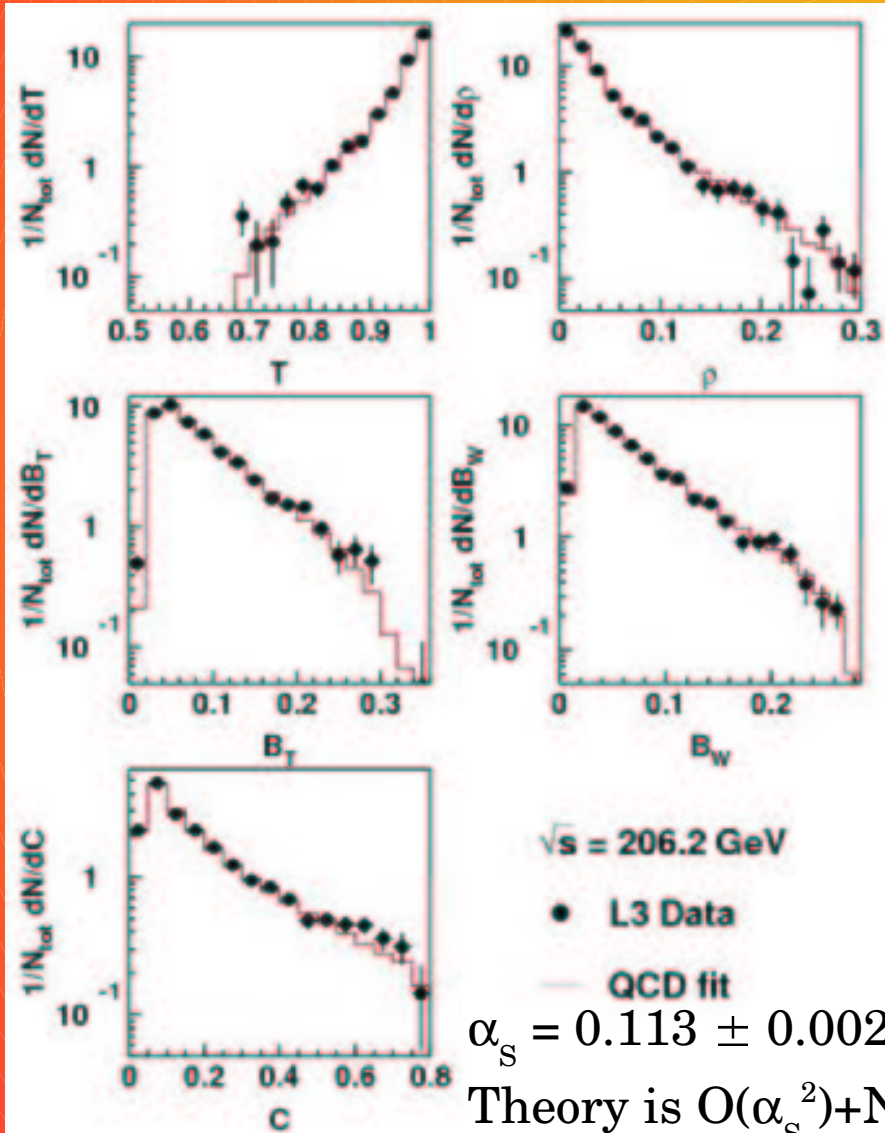


Background

τ -pairs
 2-photon
 ISR
 τ -pairs
 2-photon
 ISR
 τ -pairs
 2-photon
 ISR
 4 fermion

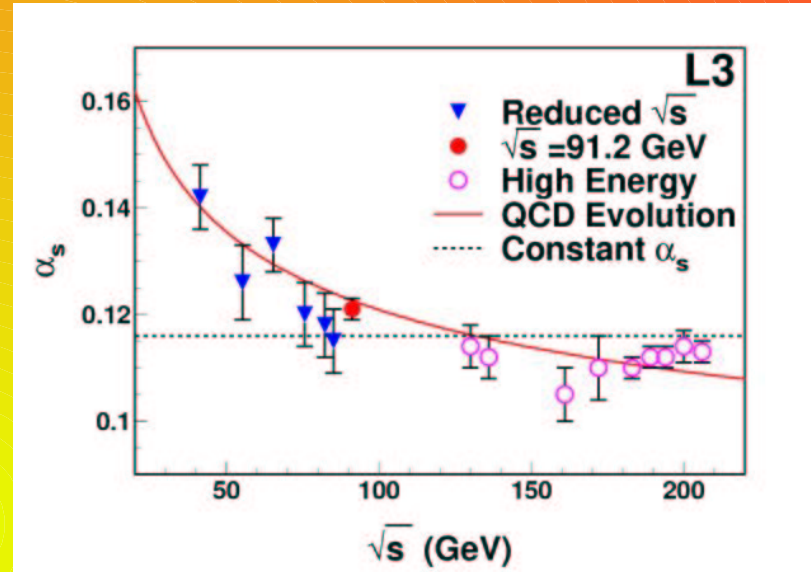
hep-ex/0001023

2 α_s at LEP 2: L3



$$\alpha_s = 0.113 \pm 0.002 \pm 0.005$$

Theory is $O(\alpha_s^2)$ +NLLA QCD



$$\alpha_s(M_Z) = 0.123 \pm 0.001 \pm 0.006$$

$$\chi^2/\text{d.o.f.} = 18/15 \quad (= 52/15 \alpha_s \text{ const})$$

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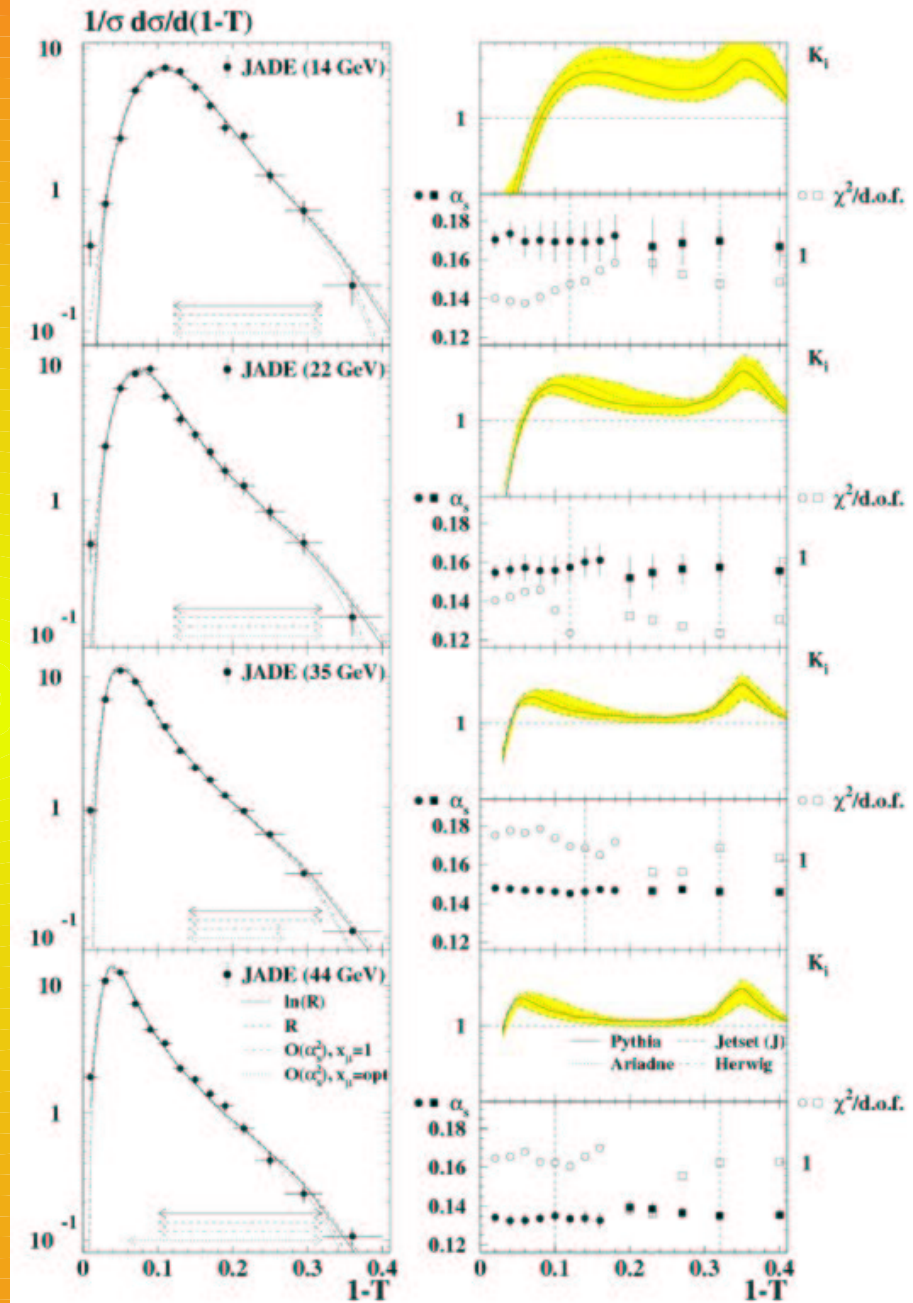
2 α_s from JADE

Re-analysis of JADE data (2002):

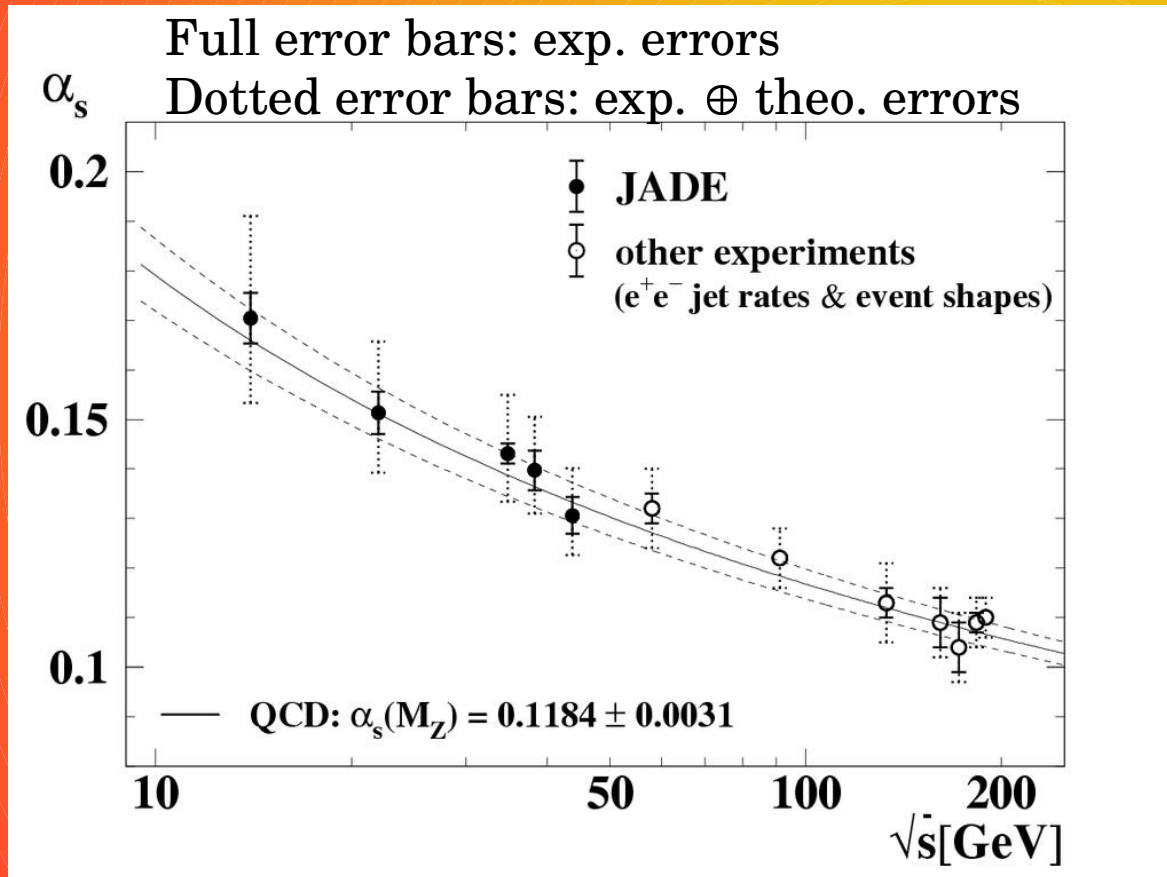
- ☺ new MC generators
- ☺ more MC statistics
- ☺ subtract b-quark events
- ☺ up-to-date QCD calculations

JADE note 144, PITHA 03/01

\sqrt{s} [GeV]	$\alpha_s(\sqrt{s})$	$\Delta \alpha_s$
14	0.170	± 0.019
22	0.151	± 0.013
35	0.146	± 0.012
44	0.131	± 0.009



2 Running of α_s

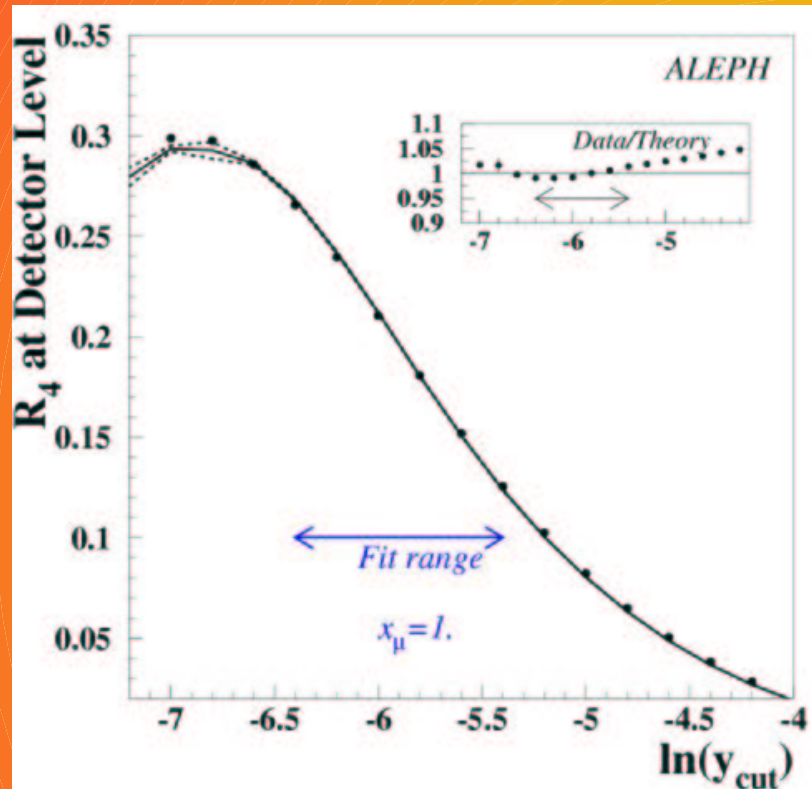


Use data from 14 to
189 GeV, exp. errors only:

$P(\chi^2)$ of QCD fit = 75 %

$P(\chi^2)$ of $\alpha_s = \text{const} \sim 10^{-5}$

2 α_S from 4-jet events



Use $2.5 \cdot 10^6$ Z^0 decays, Durham jet algorithm and $O(\alpha_S^3)$ +NLLA (R-match) theory

Total corrections $< 10\%$, some cancellation of det. and had. Corr.

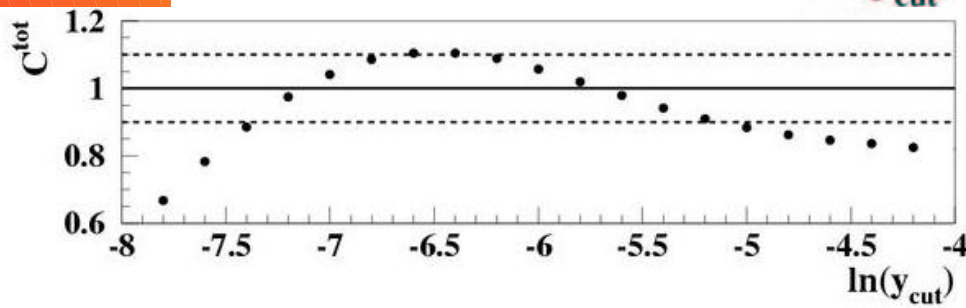
Result (fixed RS $x_\mu = 1$):

$$\alpha_S(M_Z) = 0.1170 \pm 0.0022$$

(DELPHI NLO (prelim):

$$\alpha_S(M_Z) = 0.1178 \pm 0.0029, x_\mu^2 = 0.015)$$

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DELPHI 2001-059 CONF 487



2 Running b quark mass

$$m_b(Q^2) \approx M_b \cdot \left(\alpha_S(Q^2) \frac{1}{\pi} \right)^{12/23}$$

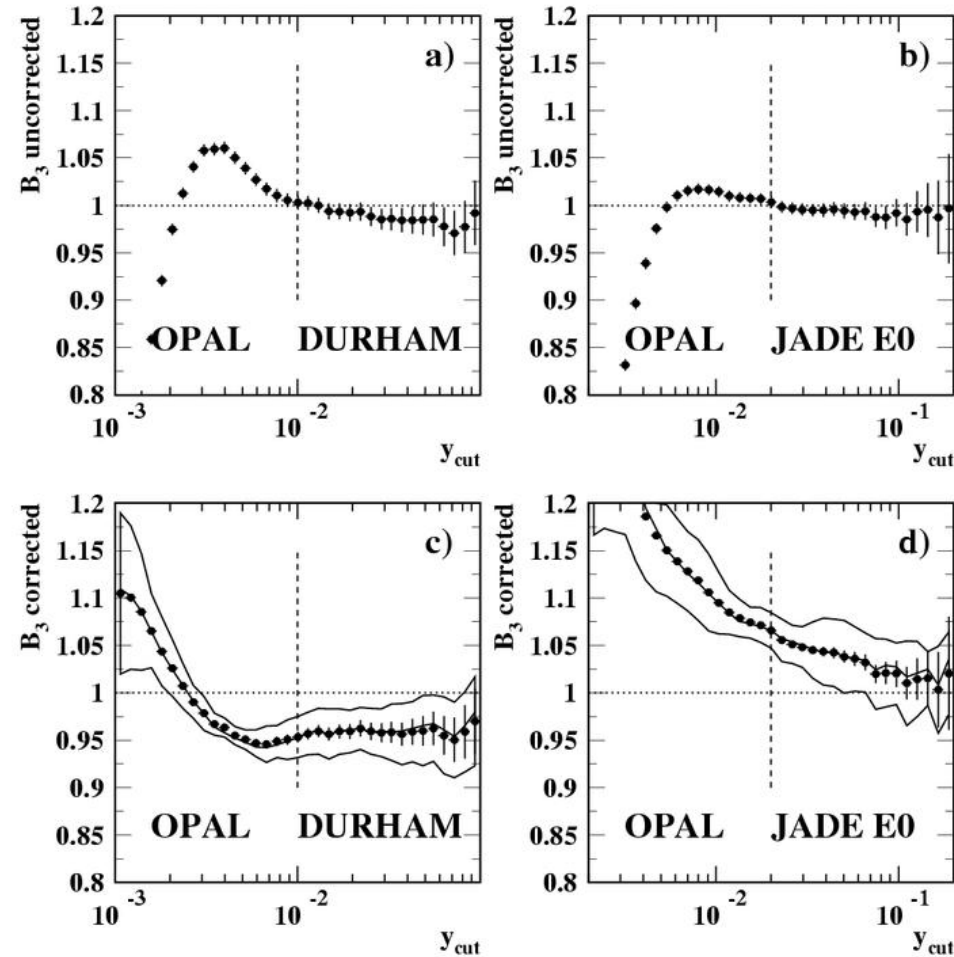
(known in NNLO)

Expect $m_b(M_Z) \sim 3 \text{ GeV}$

Study e.g. Ratio of
3-jet rates $R_3(M_Z)$:

$$B_3(M_Z) = \frac{R_3^b(M_Z)}{R_3^{udsc}(M_Z)}$$

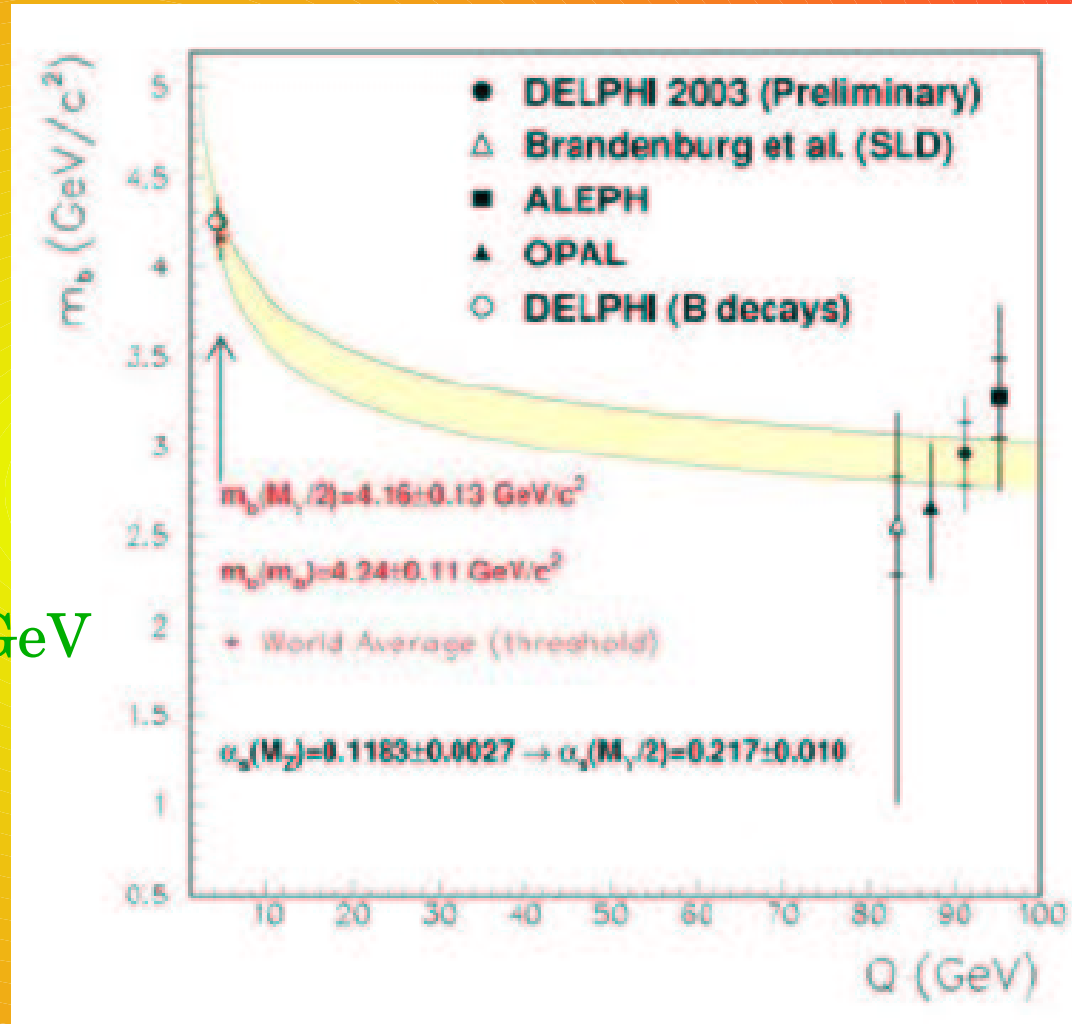
Eur. Phys. J. C 21 (2001) 411-422



2 Running b quark mass

	$m_b(M_Z)$ [GeV]
ALEPH	3.27 ± 0.52
DELPHI*	2.96 ± 0.32
OPAL	2.67 ± 0.38
SLD	2.56 ± 1.04
my average*	2.89 ± 0.26

$m_b(m_b) - m_b(M_Z) = 1.35 \pm 0.28 \text{ GeV}$
 with $m_b(m_b) = 4.24 \pm 0.11$
 → non-zero by 4.8 s.d.

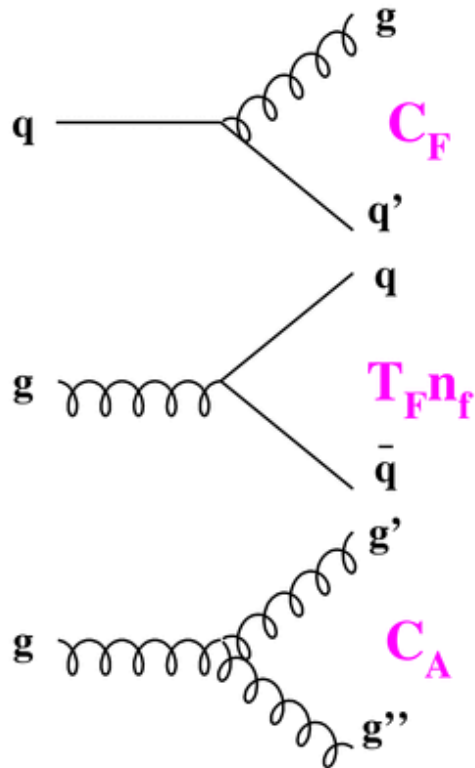


Eur. Phys. J. C18 (2000) 1,
 DELPHI 2003-024 CONF 644,
 Eur. Phys. J. C21 (2001) 411,
 Phys. Lett. B468 (1999) 168

* preliminary

3 QCD Gauge Structure

Experimental tests of the QCD gauge symmetry



QCD has 3 vertices in $O(\alpha_s^2)$

→ Decomposition of cross sections

$$A(\mathbf{y}) \sim C_F$$

$$B(\mathbf{y}) = C_F B_{C_F} + C_A B_{C_A} + T_F n_f B_{n_f}$$

$$C(\mathbf{y}) = C_F^2 C_1 + C_A^2 C_2 + T_F n_f^2 C_3 + C_F C_A C_4 + C_F T_F n_f C_5 + C_A T_F n_f C_6$$

$$NLLA = NLLA(C_F, C_A, n_f)$$

$$C_F = 4/3, C_A = 3, T_F \cdot n_f = 1/2 \cdot 5 \text{ in SU(3) QCD}$$

3 4-jet Events

At LO (α_s^2) 2-fermion+2-boson and 4-fermion 4-jet final states

Gluon decay sensitive to C_A and $T_{f f}$

Select hadronic Z decays to 4-jet final states

Construct angular correlations from
energy-ordered 3-momenta p_i of the four jets:

$$\chi_{\text{BZ}} = \sphericalangle(\mathbf{p}_1 \times \mathbf{p}_2, \mathbf{p}_3 \times \mathbf{p}_4)$$

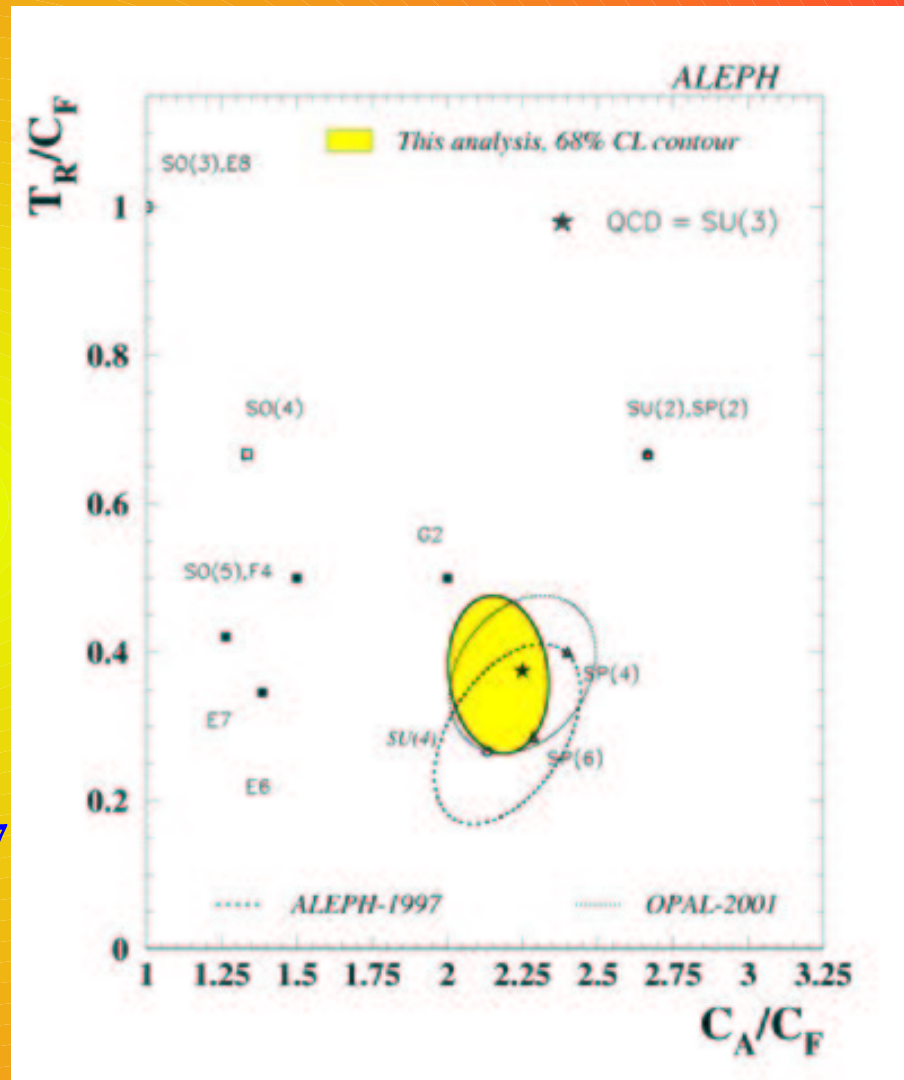
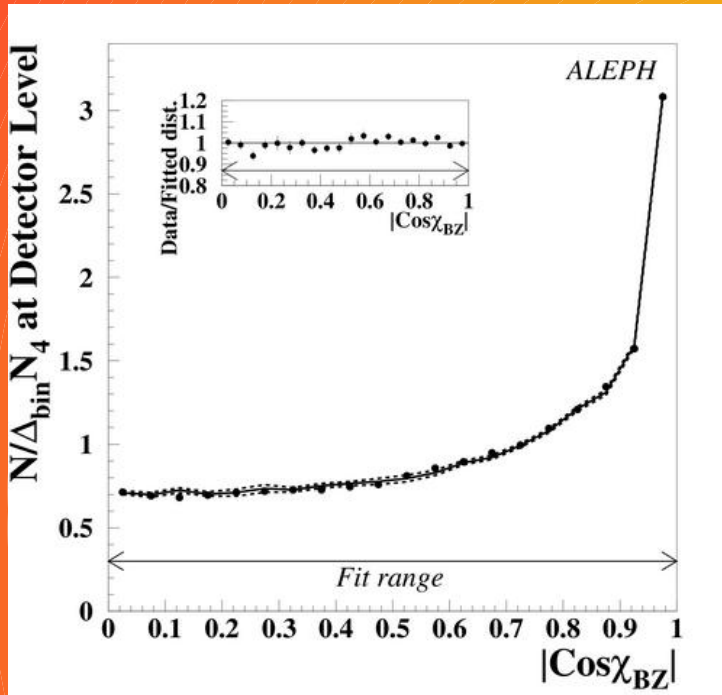
$$\Phi_{\text{KSW}} = 1/2(\sphericalangle(\mathbf{p}_1 \times \mathbf{p}_4, \mathbf{p}_2 \times \mathbf{p}_3) + \sphericalangle(\mathbf{p}_1 \times \mathbf{p}_3, \mathbf{p}_2 \times \mathbf{p}_4))$$

$$\theta_{\text{NR}} = \sphericalangle(\mathbf{p}_1 - \mathbf{p}_2, \mathbf{p}_3 - \mathbf{p}_4)$$

$$\alpha_{34} = \sphericalangle(\mathbf{p}_3, \mathbf{p}_4)$$

NLO (α_s^3) corrections available (MENLO PARC, DEBRECEN)

3 4-jet Events



OPAL

ALEPH

$$\alpha_S(M_Z) 0.120 \pm 0.023$$

$$0.119 \pm 0.027$$

$$C_A 3.02 \pm 0.55$$

$$2.93 \pm 0.60$$

$$C_F 1.34 \pm 0.26$$

$$1.35 \pm 0.27$$

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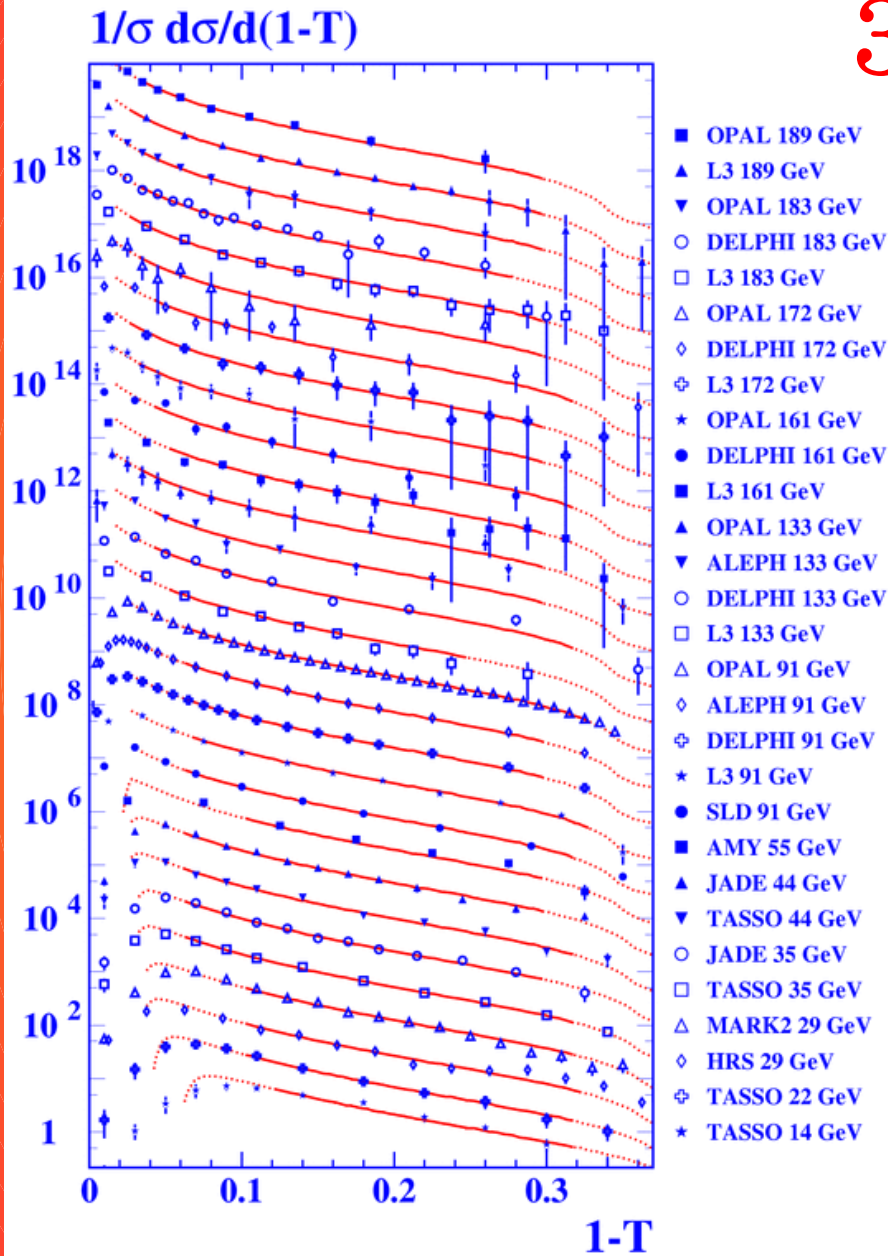
3 Event Shape Fits

Event shapes 14 to 189 GeV

NLO+NLLA QCD (ln(R)-matching)

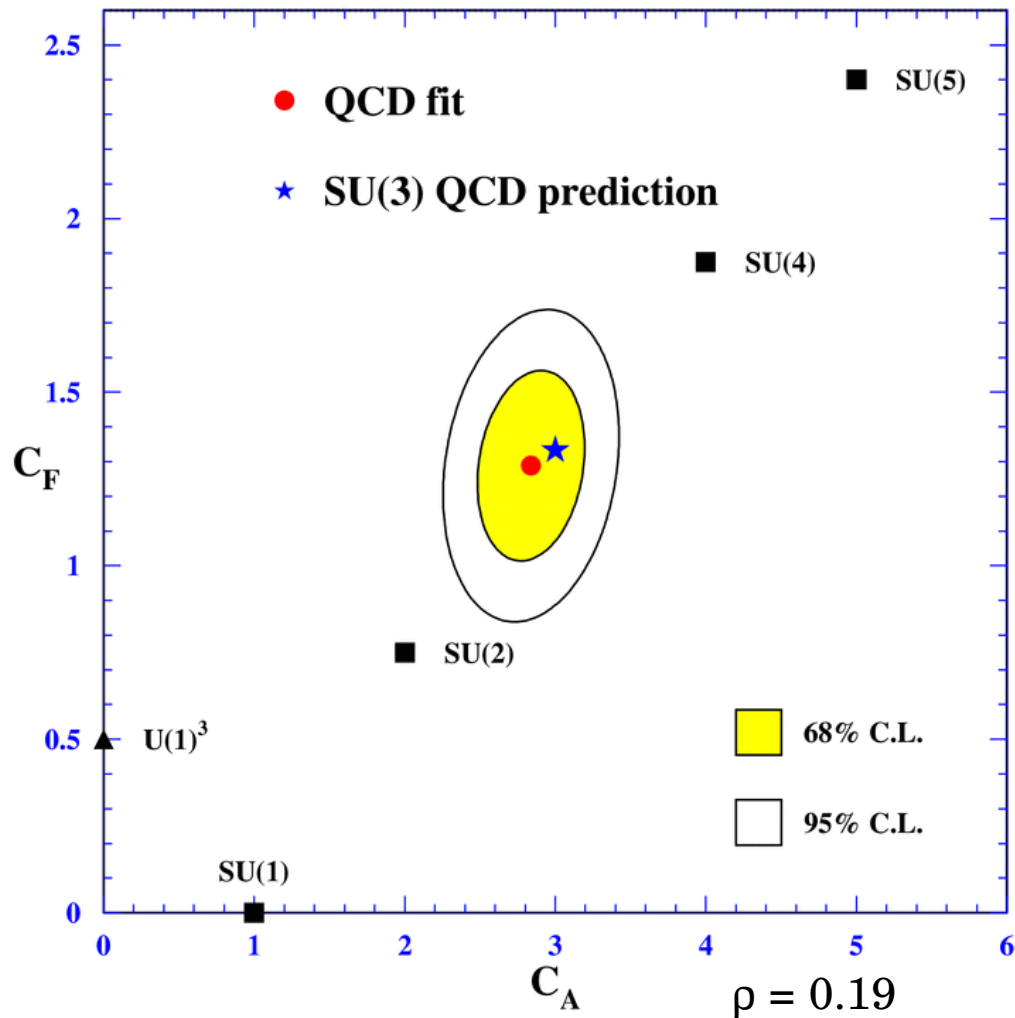
power corrections for had. effects,
with explicit colour factors

Sim. fits of α_S , C_A and C_F , α_0 fixed:
→ stable with 1-T and C



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3 Event Shape Fits



$$C_A = 2.84 \pm 0.24$$

$$C_F = 1.29 \pm 0.18$$

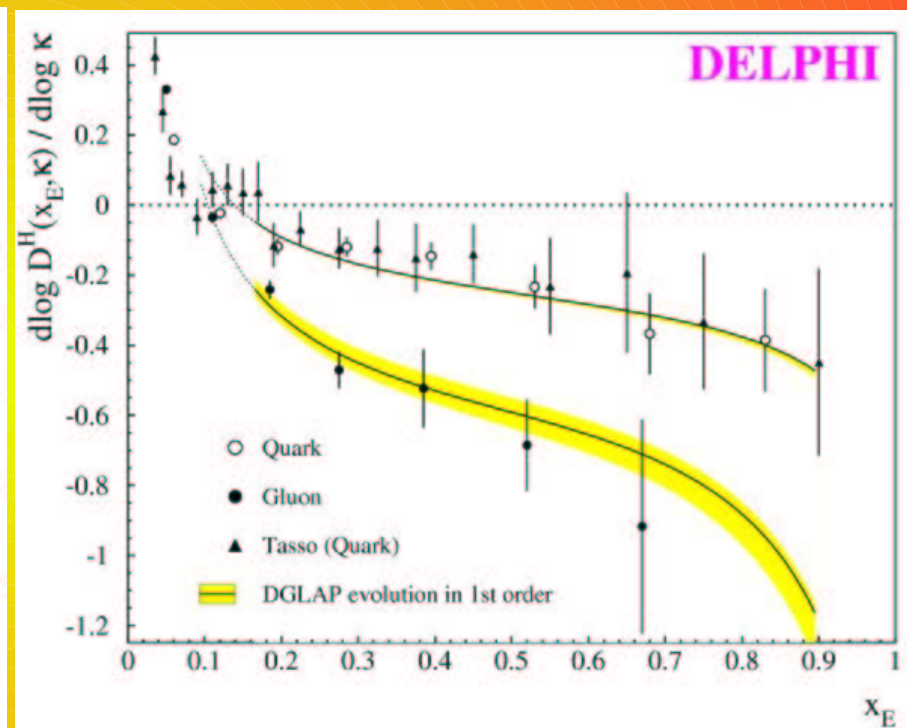
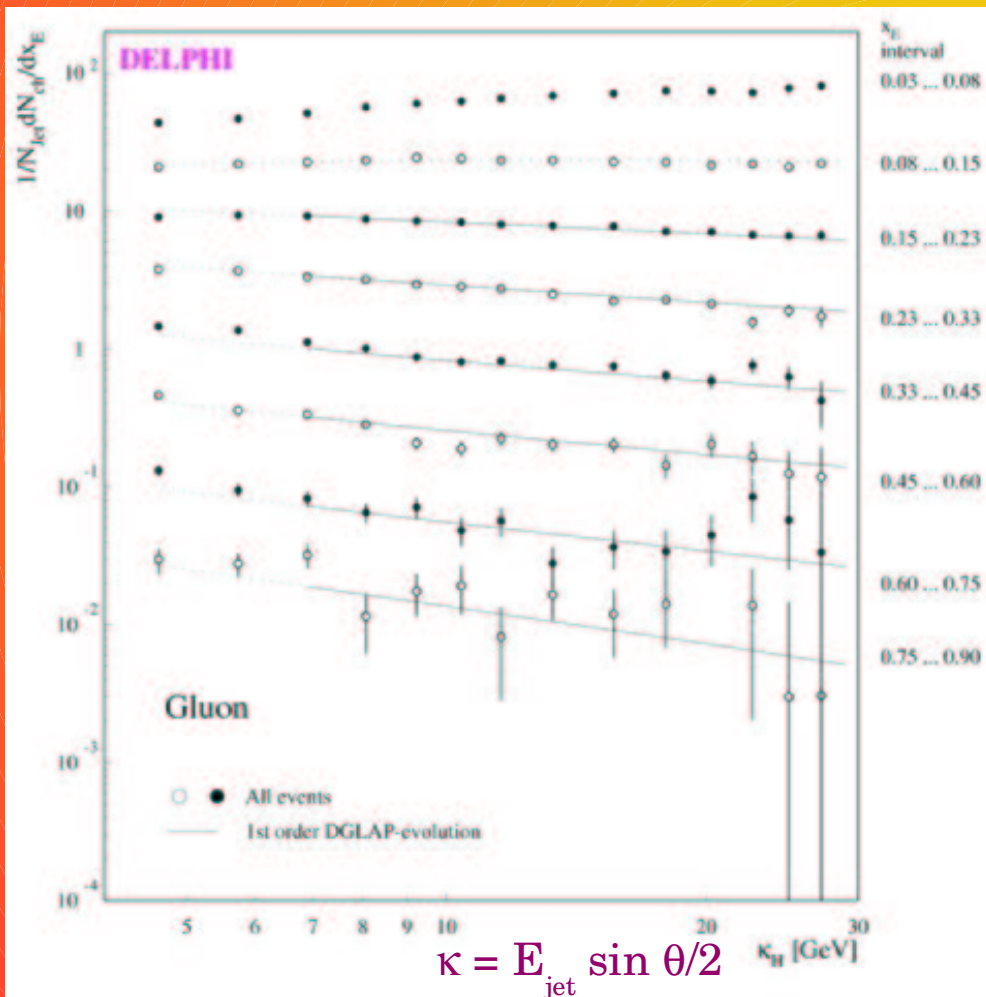
$$\alpha_S(M_Z) = 0.119 \pm 0.010$$

Results consistent with
4-jets, errors comparable
or smaller

Eur. Phys. J. C 21 (2001) 199-210

3 Gluon vs Quark Jets

Ratio of scaling violation of FFs in gluon and quark jets
 Exclusive jets in Z decays with b-quark-jet tagging



$$C_A = 3.01 \pm 0.22$$

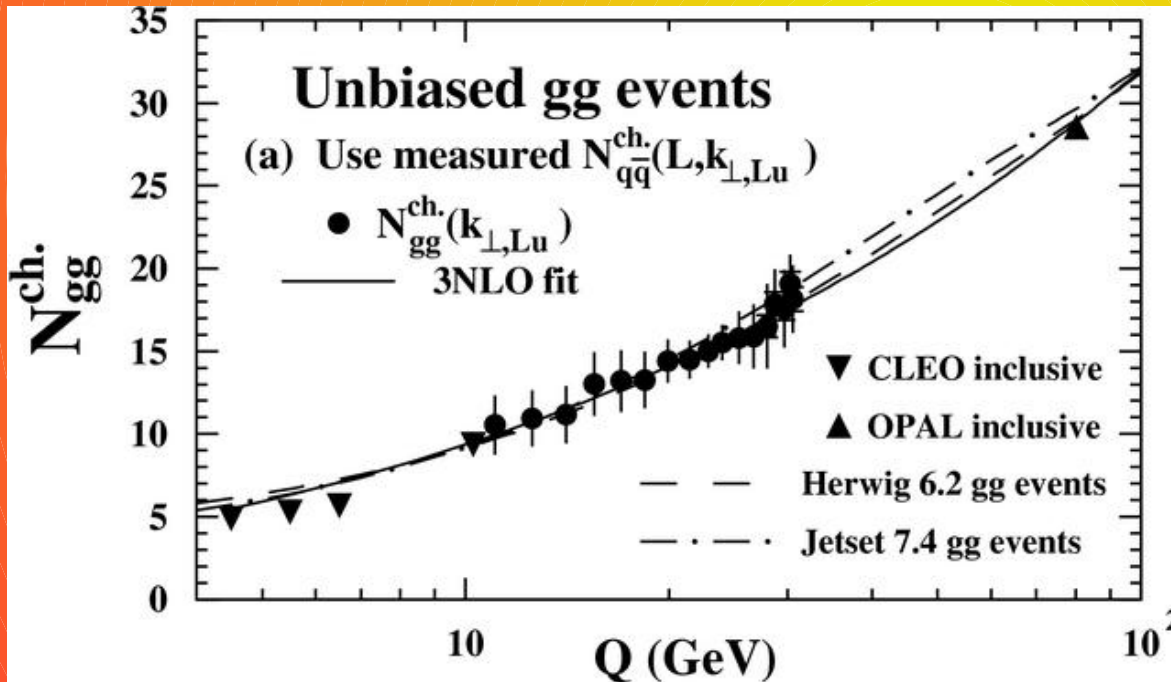
Eur. Phys. J. C13 (2000) 573

3 Gluon vs Quark Jets

$\langle n_{ch} \rangle$ evolution from unbiased gluon jets

Study $\langle n_{ch} \rangle$ as function of 3-jet resolution scale k_{\perp} with DURHAM

Extract unbiased $\langle n_{ch} \rangle_{gg}$ using $\langle n_{ch} \rangle_{qq}$ and MLLA QCD

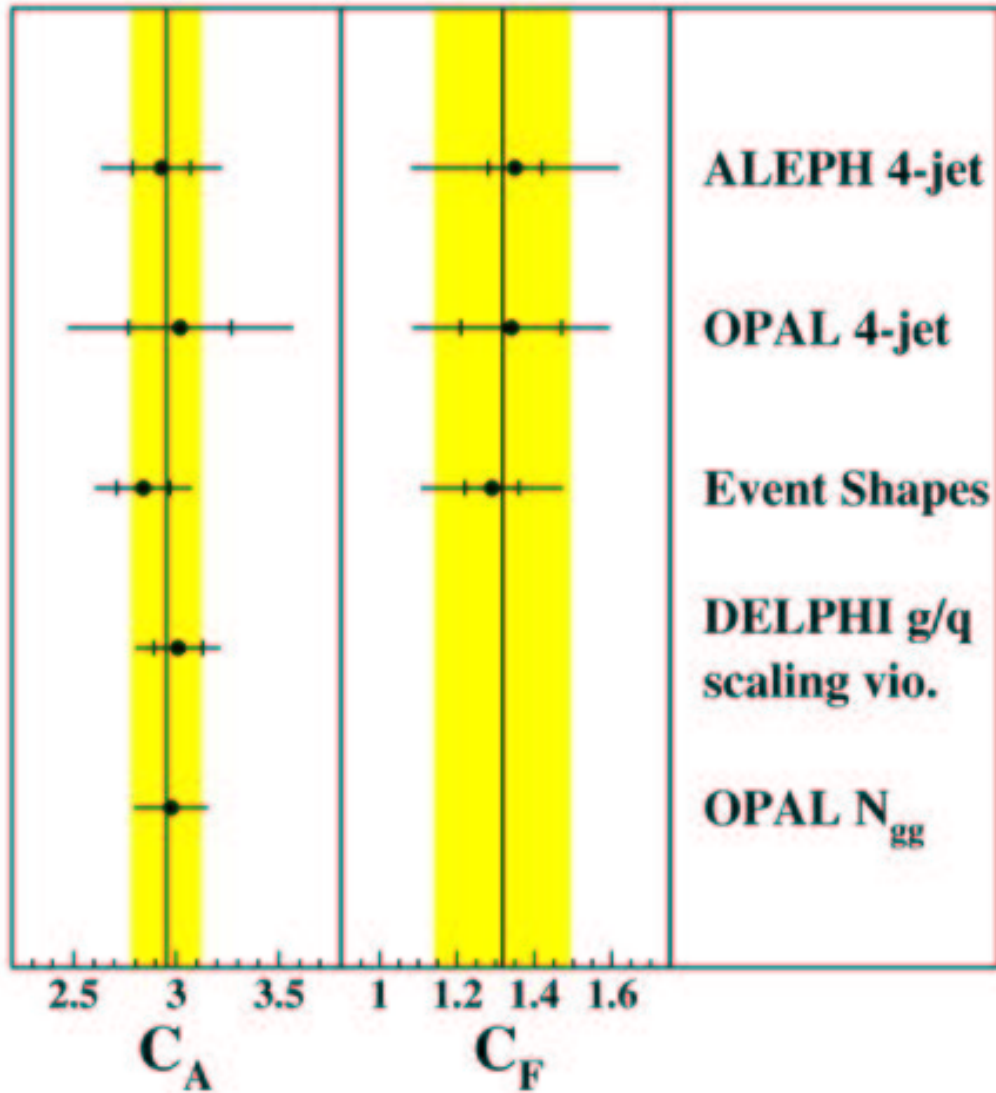


$$C_A = 2.98 \pm 0.18$$

$$k_{\perp, Lu} = \ln(s_{qg} s_{q\bar{q}} / (s \Lambda^2))$$

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3 QCD Colour Factors



My averages* :

$$C_A = 2.95 \pm 0.01 \pm 0.17$$

$$C_F = 1.32 \pm 0.05 \pm 0.17$$

QCD: $C_A = 3, C_F = 4/3$

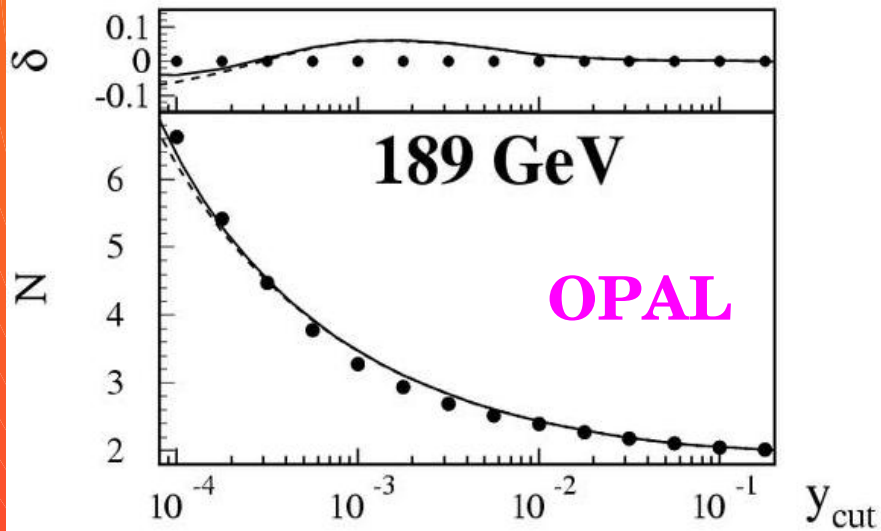
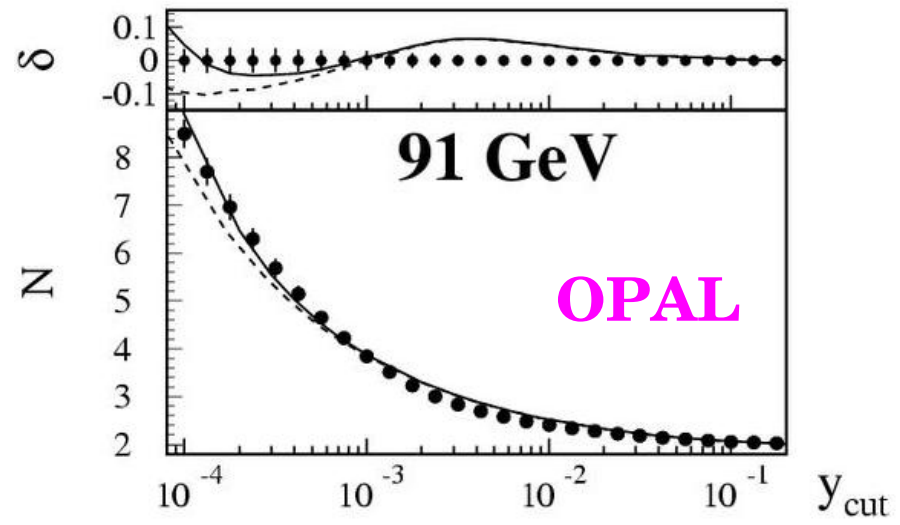
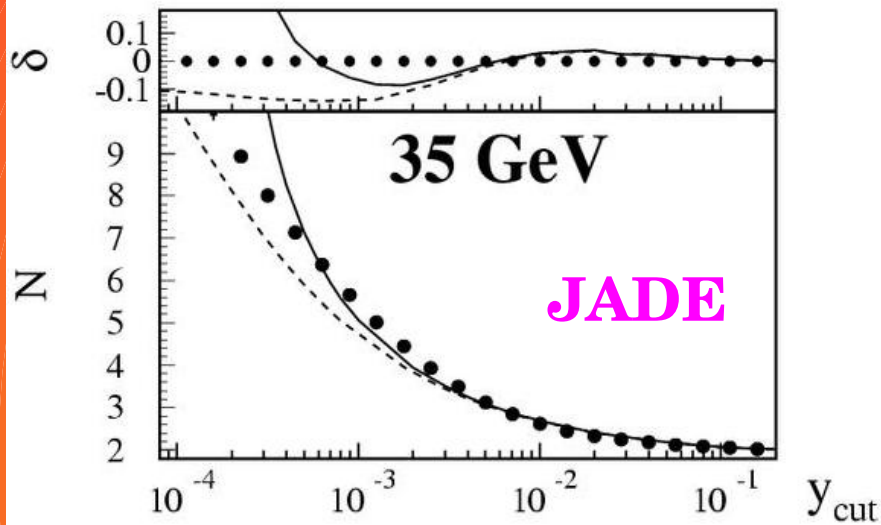
Good agreement, understand gauge structure at ~10% level

* preliminary

Summary

- Jet Physics from $\sqrt{s} = 14$ to 207 GeV
 - Precision measurements of α_s
 - Study running of α_s
 - Measure running m_b
- Gauge structure of QCD from jets
 - 4-jet angular correlations, event shapes, gluon FF s.v., $\langle n_{ch} \rangle_{gg}$
 - Can measure C_A and C_F to about 10%
- QCD for jets in very good shape!

2 Soft QCD Tests: LPHD



$$N = \langle N_{\text{jet}} \rangle \text{ (DURHAM)}$$

Lines are MLLA QCD prediction without (solid) and with (dashed) simple quark mass correction

Eur. Phys. J. C 17 (2000) 19-51

2 Quark vs Gluon Jets: x_E

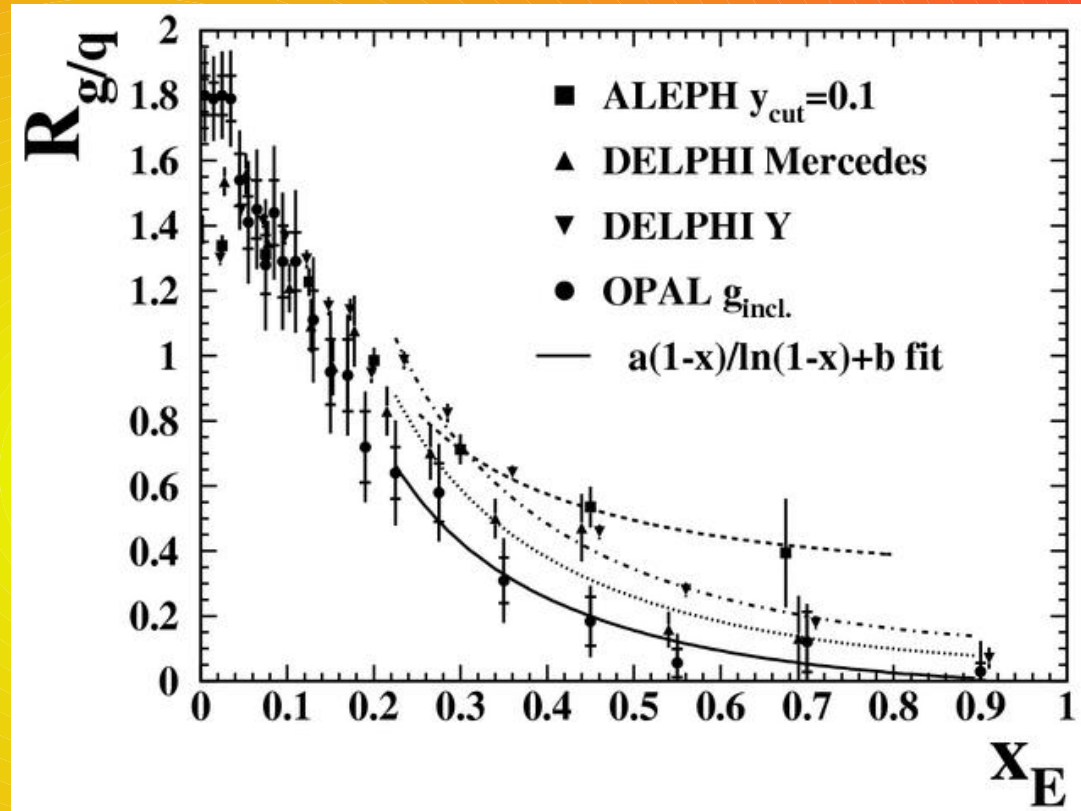
LLA QCD prediction ('78):

$$R_{g/q} \sim (1-x)/\ln(1-x) \text{ for } x \approx 1$$

Never tested so far.

Can now compare with data,
use total errors, $x_E > 0.2$:

	χ^2/dof
ALEPH	0.03/1
DELPHI M	4.3/4
DELPHI Y	25/5
OPAL g_{incl}	1.3/5



Strong g/q effect in x_E spectra

LLA QCD consistent with data

Better (NLLA) prediction?